# Solution Dynamics and Self-Organization

Professor William S. Price Professor of Nanotechnology University of Western Sydney E-mail: w.price@uws.edu.au

## Outline

- A. Solution Dynamics and Self-Organization.
- B. The Pulsed Gradient Spin Echo (PGSE) NMR method for measuring translational diffusion.
- C. Some Examples
  - 1. Supercooled Water
  - 2. Isolated Water Molecules
  - 3. Alcohol Water Systems
  - 4. Drug Binding
  - 5. Aggregation and Crystallization of Lysozyme

## **Solution Dynamics**

#### Includes:

- Association  $\rightarrow$  self organization and crystallisation
- **Binding** (e.g., drug protein or drug -DNA)
- Phase changes
- Bio-thermodynamics (e.g., macromolecular crowding effects)
- Exchange (e.g., transmembrane)

#### How a molecule interacts with its neighbours and surroundings.



## Types of Motion







Time taken to reorientate by ~ 1 radian

**Reorientational** / Correlation Time,  $\tau_c^{\dagger}(s)$ 



Different parts of molecule may have different reorientational motions, but <u>a single diffusion</u> <u>coefficient</u> characterises the whole molecule.

NMR can probe both types of motion.



## Mw and Motion

#### Translational diffusion

**Stokes-Einstein equation** (only holds at infinite dilution)

$$D = \frac{kT}{f}$$

- friction coefficient

sphere 
$$f = n\pi\eta r_{\rm s}$$

rs

n = 4 (slip), 6 (stick)

 $D \,({\rm m}^2{\rm s}^{-1}) \times 10^9$ **Species T**(**K**)  $M_{w}$ 298 2.26 18  $H_{2}O$ Glycine 298 75 1.05 298 0.67 180 glucose 95 inorganic phosphate 298 0.61 creatine phosphate 298 0.52 211 0.52 298 342 sucrose ATP 298 0.37 507 insulin 293 0.082 5700 298 0.108 14500 lysozyme hemoglobin 293 0.063 64500 tobacco mosaic virus 293 0.005 4000000



Reorientational motion

$$Mw \uparrow \tau_c \uparrow T_2 \downarrow$$



### Diffusion as a Probe of Organization

#### Advantages:

Organization and association generally involve changes in molecular weight and hydrodynamic properties  $\rightarrow$  diffusion is a natural probe of such phenomena.

Data analysis is facilitated by diffusion being a property of the **entire molecule** (excluding exchangeable groups)

#### **Complications:**

Finite Solute Concentrations: Inter-particle collisions and interactions (i.e., 'obstruction effects') also influence the measured diffusion coefficient. Nuisance <u>OR</u> source of information?





### PGSE NMR Diffusion Measurements

Using spatially well-defined magnetic field gradients to spatially encode the translational motion of spins – this includes diffusion, flow, turbulence ....

PGSE NMR measures self-diffusion not mutual diffusion.

Also known as q-space imaging, PGSE (Pulsed Gradient Spin-Echo), DOSY (Diffusion Ordered Spectroscopy) or NMR diffusometry.



### The Mechanics of NMR Diffusion Measurements



### The PGSE NMR Experiment



### What About Signal Attenuation due to Relaxation?



Normally, the attenuation due to relaxation is normalised out.

$$E = \frac{S(g)}{S(0)} = \frac{\exp\left(-\gamma^2 g^2 D(\Delta - \delta/3)\right) \exp\left(-2\tau/T_2\right)}{\exp\left(-2\tau/T_2\right)} = \exp\left(-\gamma^2 g^2 D(\Delta - \delta/3)\right)$$

Echo Signal Attenuation

Unfortunately, this 'elegant' solution is not general - it only holds for a single component.



### A Summary of the Characteristics of PGSE • "Rule of Thumb" $M_{w} \uparrow D \downarrow$ PGSE can measure diffusion in the range of $10^{-9} - 10^{-14} \text{ m}^2\text{s}^{-1}$ . H<sub>2</sub>O solid polymer If the mean square displacement during the experiment $(\Delta \sim 10 \text{ ms} - 1 \text{ s})$ is such that a sufficient population of spins make contact with the boundaries $\Rightarrow$ complicated non-exponential attenuation profiles. Experimentally this corresponds to barriers with characteristic distances, $R \square 100 \mu m$ . At finite concentrations the diffusing species obstruct each other $\Rightarrow D \downarrow$

Differential relaxation weighting is a problem in polydisperse systems.

The combination of these effects can complicate data interpretation



11

## SUPERCOOLED WATER

• What is the nature of the water  $\leftrightarrow$  ice transition?

Self-nucleation temperature is about 231 K.

Metastable 'Grey area' from 273 to 231 K.

PGSE is one of the few applicable techniques.



## Sample for Supercooled Water Diffusion Measurements



### Supercooled <sup>1</sup>H<sub>2</sub>O Diffusion



Fractional Power Law (FPL) and Vogel-Tamman-Fulcher (VTF) Relations

**FPL equation** (sharp transition from water to ice)

$$D = D_0 T^{1/2} \left( \frac{T}{T_s} - 1 \right)^{\gamma}$$

 $T_{S}$ : low temperature limit (singularity)  $D_{0}, \gamma$ : fitting parameters

VTF equation (smooth transition)

$$D = D_0 \exp\left\{-B/(T-T_0)\right\}$$

 $T_0$ : related to the glass transition temperature  $D_0, B$ : fitting parameters

## Modeling <sup>1</sup>H<sub>2</sub>O Diffusion Using the FPL and VTF Relations



## Apparent Activation Energy of <sup>1</sup>H<sub>2</sub>O Diffusion





### **ISOLATED-WATER MOLECULES**

- Anomalous behaviour of liquid water arises from hydrogen bond network.
- Water dissolved in a hydrophobic solvent 'isolated' water molecules.
- No hydrogen bonding between water molecules.
- Studied the diffusion (<sup>17</sup>O PGSE) and <sup>17</sup>O longitudinal relaxation  $(T_1)$  of H<sub>2</sub><sup>17</sup>O dissolved in nitromethane.
- Non-standard', low  $\gamma$  nuclei are now becoming accessible to PGSE measurement with the increasingly larger applied gradients available.



## <sup>17</sup>O PGSE and Relaxation Measurements



#### Correlation between Reorientational Correlation Time and Diffusion in the Hydrodynamic Continuum Model



## ALCOHOL-WATER

■ Alcohols are amphiphilic → complicated solution chemistry.

Methanol, Ethanol and *tert*-Butanol differ only in the size of the alkyl group.

Primordial" lipids - models for micelle assembly.



## Diffusion in the Methanol-Water System at 298 K





## Diffusion in the Ethanol-Water System at 298 K





## Diffusion in the *tert*-Butanol-Water System at 298 K





## Arrhenius Activation Energy for Diffusion



## Stokes-Einstein Analysis of the Methanol System at 298 K



## Stokes-Einstein Analysis of the Ethanol System at 298 K











## Alcohol-Water Summary

- At low *x*<sub>A</sub> the alcohol molecules associate due to hydrophobic hydration. The alcohol molecules sit at the centre of hydration shells.
- As  $x_A$  increases there comes a point where there are insufficient H<sub>2</sub>O to form the shells.
- The three alcohols have quite different properties.
- *tert*-Butanol has the strongest hydrophobic hydration but the weakest H-bonding.
- Ideally, we would like to study the very low  $x_A$ .



**DRUG BINDING** 

#### Diffusion is a very powerful method for screening drugs and characterizing their binding properties.



### The Practicalities of Diffusion-based Binding Assays

#### Wish to determine:

- i. Is there any binding.
- ii. Dissociation constants.
- iii. Decide if there are one or more classes of binding constants.

#### To do so it is necessary to:

- i. Accurately measure D of the drug over large concentration ranges (esp. v. low concentrations) ideally in non-deuterated samples (i.e., in  ${}^{1}\text{H}_{2}\text{O}$  not  ${}^{2}\text{H}_{2}\text{O}$ ).
- ii. Remove the signals of the receptor.
- iii. Consider the effects of NMR relaxation on the measurement.



### The Basis of Diffusion-based Binding Assays protein $K_d$ drug $D_b = D$ of protein (v. slow) (~ unchanged by drug binding) $D_f = D$ of drug (fast)

If the exchange is fast on the NMR timescale, <u>the observed drug</u> <u>diffusion coefficient D</u>, will be the population weighted average of the diffusion coefficients:  $D = P_b D_b + P_f D_f$ 

Can use a diffusion filter to detect binding or a more detailed analysis to determine the dissociation constant  $(K_d)$ .

The use of NMR diffusion measurements to study drug binding is sometimes referred to as "Affinity NMR".

General ref.: Encyclopedia of Nuclear Magnetic Resonance (2002) 9, 364-374.



### Effects of Ligand Relaxation

The bound and free states of the drug have different relaxation rates.





Kärger et al Adv. Magn. Reson. (1988) 12, 1-89.

#### **Relaxation affects the population weighting:**

- Ignoring it in the data analysis will result in incorrect answ
- Using it provides and additional source of information.





A Hahn-based sequence is preferable to a Stimulated Echo-based PGSE sequence due to: (1) better removal of the protein resonances due to relaxation, (2) larger drug signal and (3) no complications from crossrelaxation effects.

Echo signal 
$$\rightarrow S(g) = M_0 \exp\left(-\gamma^2 g^2 D\left(\Delta - \delta/3\right)\right) \exp\left(-2\tau/T_2\right)$$

initial magnetization

Attenuation due to Diffusion

Attenuation due to Relaxation



#### Salicylate binding to BSA



### Using Q-Switching to counter Radiation Damping

The advantages of Q-switching (i.e., the rf circuitry is effectively disconnected) during acquisition are well-known.

Less well-known are the advantages of switching during the sequence.





## PROTEIN ASSOCIATION

- Involved in normal physiology and in disease (e.g., cataracts, Alzheimer's disease).
- Aggregation is the initial step in the crystallisation process.
- Proteins are both colloids and polymers.
  ⇒ need to consider size and electrostatic interactions



## Aggregation of Lysozyme

Lysozyme - forms a complicated polydisperse system.



Its aggregation state is sensitive to the solution environment (e.g., salt concentration, pH).

The spectra of the different oligomeric states <u>overlap</u>.



#### **Calculation of Protein Diffusion** How to Analyse Polydisperse Monomer/ Oligomer Protein PGSE Data? **Hydrodynamics** Aggregate Distribution **Crowding**/ Obstruction **PGSE Measurement** Effects of Protein Diffusion Ensemble Ensemble Averaging Averaging **Experimental** Theoretical Diffusion Diffusion Coefficient Coefficient



**Theoretical** 

### PGSE of a Polydisperse System

#### Assume slow exchange between the different oligometric states w.r.t. $\Delta$ .



### Ensemble Averaging of the Diffusion Coefficients



## Modelling the Oligomer Hydrodynamics

- Monomers and higher oligomers have complex shapes.
- Models (numerical and analytical) do exist.
- However, given the quality of the diffusion data and lack of knowledge of the oligometric shapes  $\Rightarrow$  assume spherical shapes.





### Importance of Charge Effects II



## Importance of Charge Effects III



### Two Models for the Effects of Obstruction on Diffusion in Lysozyme Solution

Current models for obstruction

do <u>not</u> include:

1. Aggregation effects

2. Electrostatics



### The Theoretical Diffusion Coefficient

### Combining all the steps and convenient fudges:

Includes concentration effects (i.e., obstruction)  $\langle D \rangle_{W}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C} (C) = \langle D \rangle_{W} f_{C} (C)$ Sum over the different oligomeric states Mole fraction (from aggregation model) Sum over the different  $\langle D \rangle_{W}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C} (C) = \langle D \rangle_{W} f_{C} (C)$ Sum over the different  $\langle D \rangle_{W}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C} (C) = \langle D \rangle_{W} f_{C} (C)$ Sum over the different  $\langle D \rangle_{W}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C} (C) = \langle D \rangle_{W} f_{C} (C)$   $\langle D \rangle_{W}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C} (C) = \langle D \rangle_{W} f_{C} (C)$ Sum over the different  $\langle D \rangle_{W}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C} (C) = \langle D \rangle_{W} f_{C} (C)$  $\langle D \rangle_{W}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C} (C) = \langle D \rangle_{W} f_{C} (C)$ 

The inclusion of ensemble averaging makes this equation identical to that obtained using the fast exchange but without ensemble averaging

## Lysozyme Aggregation



## What Happens at Higher Protein Concentrations ?

# With reasonably small aggregates neglecting relaxation weighting is 'reasonable'.

However, with more polydisperse systems <u>it must be</u> <u>considered</u>.

$$\left\langle D\right\rangle_{W,R}^{C} = \sum_{i} \alpha_{i} D_{1}^{0} i^{-\frac{1}{3}} f_{C}(C) \underbrace{\exp(-2\tau/T_{2,i})}_{\bigwedge} = \left\langle D\right\rangle_{W,R} f_{C}(C)$$
Relaxation

It has the effect of a high molecular weight filter with a very broad cut-off.



### Probing the Time-Dependence of Aggregation

As aggregation proceeds the larger aggregates (~ 'solid' phase) become 'NMR invisible' and PGSE measures <u>only those still in solution</u>.

- The protein remaining in solution diffuses faster due to less obstruction.
- Gradient strength permitting, the relaxation weighting can be 'tuned' to different  $M_w$  ranges.

 $\Rightarrow$  PGSE provides a means to studying the timedependence of aggregation.

### Time-Dependence of Lysozyme Aggregation I

53





## Time-Dependence of Lysozyme Aggregation III

When the sample tube was removed at the end of the experiment lysozyme crystals were visible.

Initial solution = 5 mM Lysozyme

Lysozyme crystals are invisible to PGSE NMR





## Using PGSE to Probe the Time-Dependence of Aggregation

Lysozyme	$\left\langle D(t_0) \right\rangle_W^C$	$\left\langle D(t_{\infty}) ight angle _{W}^{C}$	t <sub>sigm</sub>	Slope at inflection	Result
Concentration	$(\times 10^{-10} \text{ m}^2 \text{s}^{-1})$	$(\times 10^{-10} \text{ m}^2 \text{s}^{-1})$	<b>(h</b> )	(× <b>10</b> <sup>-17</sup> m <sup>2</sup> s <sup>-2</sup> )	
3 mM	$\boldsymbol{0.89 \pm 0.00}$	$\boldsymbol{1.05\pm0.00}$	66.5 ± 0.8	9.4	Small no. large crystals
5 mM	$0.72\pm0.01$	$1.03 \pm 0.00$	68.9 ± 1.2	14.8	Small no. large crystals
6 mM	$0.65\pm0.01$	$1.04\pm0.00$	$23.9 \pm 0.9$	27.4	Many small crystals
7 mM	0.61 ± 0.01	$1.03\pm0.00$	41.4 ± 0.9	27.0	Many small crystals

small no. of critical nuclei and large crystals





## **RELATED POSTERS**

□ Fröba et al (350) "Mutual Diffusion Coefficients in Fluids by Dynamics Light Scattering".

Gädke and Nestle (392) "Apparent Longitudinal Relaxation of Mobile Spins in Thin, Periodically Excited States".

Lang et al (356) "Molecular Motions of Calix[4]Arene and Thiacalix[4]Arene in Solution Studied by NMR Relaxation".

□ Marek et al (358) "ESRI Study of Diffusion Processes in Poly(2-Hydroxyethyl Methacrylate) Gels and Concentrated Solutions".

□ Fernandez et al (444) "New Options for Measuring Diffusion in Zeolites by MAS PFG NMR".

□ Schönfleder et al (470) "*NMR Studies of Diffusion and Pore Size Distribution on Water Containing Aquifer Rocks and Construction Materials*".

Grinberg (564) "Ultraslow Molecular Dynamics of Organized Fluids: NMR Experiments and Monte-Carlo simulations".

□ Roland et al (584) "Influence of Phase Transitions on the Mobility of Organic Pollutants in Synthetic and Natural Polymers".

Sagidullin et al (588) "Water Diffusion through Assymetric Polymer Membranes and Polyelectrolyte Multilayers".

## Acknowledgements

#### **NSW State Government BioFirst Award.**

- Peter Stilbs, Royal Institute of Technology, Sweden.
- Olle Söderman, University of Lund, Sweden.
- Fredrik Elwinger, GE Healthcare, Sweden.
- Voji Arata, Water Research Institute, Japan.
- Hiroyuki Ide, Ajinomoto, Japan.
- **Fumihiko Tsuchiya,** Applied Biosystems Japan.
- Cécile Vigouroux, Royal Institute of Technology, Sweden.
- Markus Wälchli, Bruker Biospin, Japan.

#### Water Suppression

One of the best suppression techniques is the WATERGATE sequence.

Selective  $\pi$  pulse (e.g., a binomial pulse) that gives a null on the solvent resonance



The WATERGATE sequence resembles a PGSE sequence except diffusion effects (i.e., signal loss) are minimized.

#### WATERGATE



**PGSE-WATERGATE** 



A Hahn-based sequence is preferable to a Stimulated Echo-based PGSE sequence due to: (1) better removal of the protein resonances due to relaxation, (2) larger drug signal and (3) no complications from crossrelaxation effects.

Echo signal 
$$\rightarrow S(g) = M_0 \underbrace{\exp\left(-\gamma^2 g^2 D\left(\Delta - \delta/3\right)\right)}_{\text{Attenuation due}} \underbrace{\exp\left(-2\tau/T_2\right)}_{\text{Attenuation due}}$$

initial magnetization

### PGSE Spectra of Salicylate in BSA Solution

The binding of salicylate to albumin governs its transport and tissue distribution.



Unless the solvent suppression is excellent, the three proton resonances appear to give different diffusion coefficients.

### Problems with NMR of Strong Signals

Strong' samples present particular difficulties to NMR measurements due to the induction of <u>radiation damping</u> effects.
Radiation damping is in effect a feedback loop between the sample magnetization and the rf coil/circuitry.



Gets worse in better spectrometers and more sensitive probes (e.g., cryoprobes). It affects both T<sub>1</sub> and T<sub>2</sub> (and therefore lineshape) and has very deleterious effects on pulse sequences – esp. PGSE sequences.
 Reducing B<sub>0</sub>, η or Q is not a solution when trying to detect small resonances.

## Radiation Damping Effects on Relaxation



The non-linear behaviour of the water makes pulse sequence design very difficult.

### Radiation Damping and the PGSE Sequence

Radiation damping effects are ~ negligible when the magnetization is gradient encoded (the vector sum of the net magnetization is zero).



The effects of radiation damping during  $t_1$  are constant but change during  $t_2$  in a complicated manner on the gradient parameters ( $\delta$ , g,  $\Delta$ ).

### Mild Radiation Damping Effects on PGSE



## Using Q-Switching

The advantages of Q-switching (i.e., the rf circuitry is effectively disconnected) during acquisition are well-known.

Less well-known are the advantages of switching during the sequence.





### Diffusive Diffraction (between parallel PLANES)

