

# Diffusional Contributions and Electrostatic Interactions during Ultrafiltration

**Andrew L. Zydney**

Department Head and Walter L. Robb Family Chair  
Department of Chemical Engineering  
The Pennsylvania State University

Diffusion  
Fundamentals



PENNSTATE

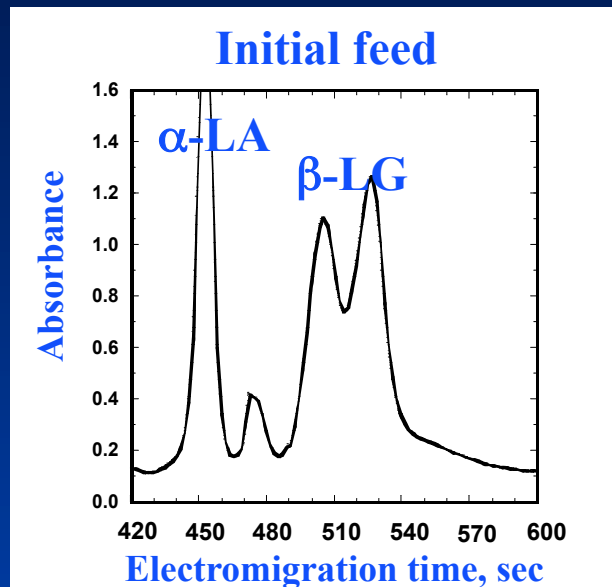


# Ultrafiltration

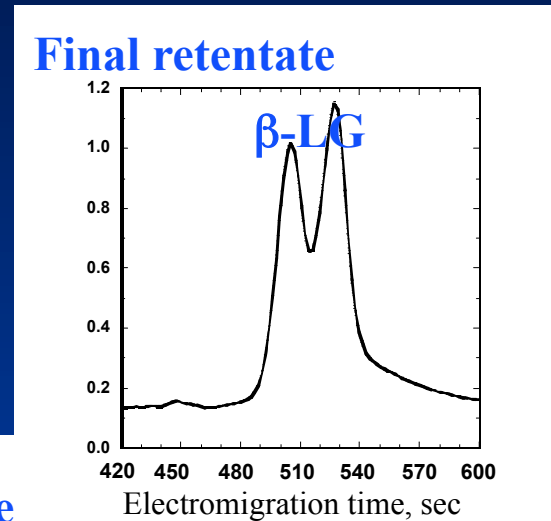
---

- Ultrafiltration is used extensively for protein concentration, buffer exchange, and desalting
  - Formulation of therapeutic proteins
  - Processing of food and beverage products
- Recent studies have demonstrated the potential of using ultrafiltration for protein separations based on different rates of protein transport across semi-permeable membranes

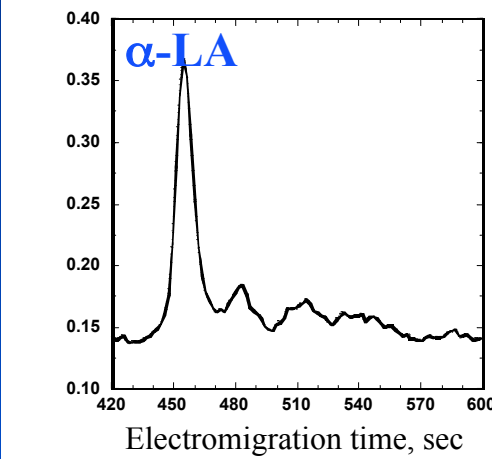
# Whey Protein Purification



Ultrafiltration  
at pH 5.5  
50 mM phosphate



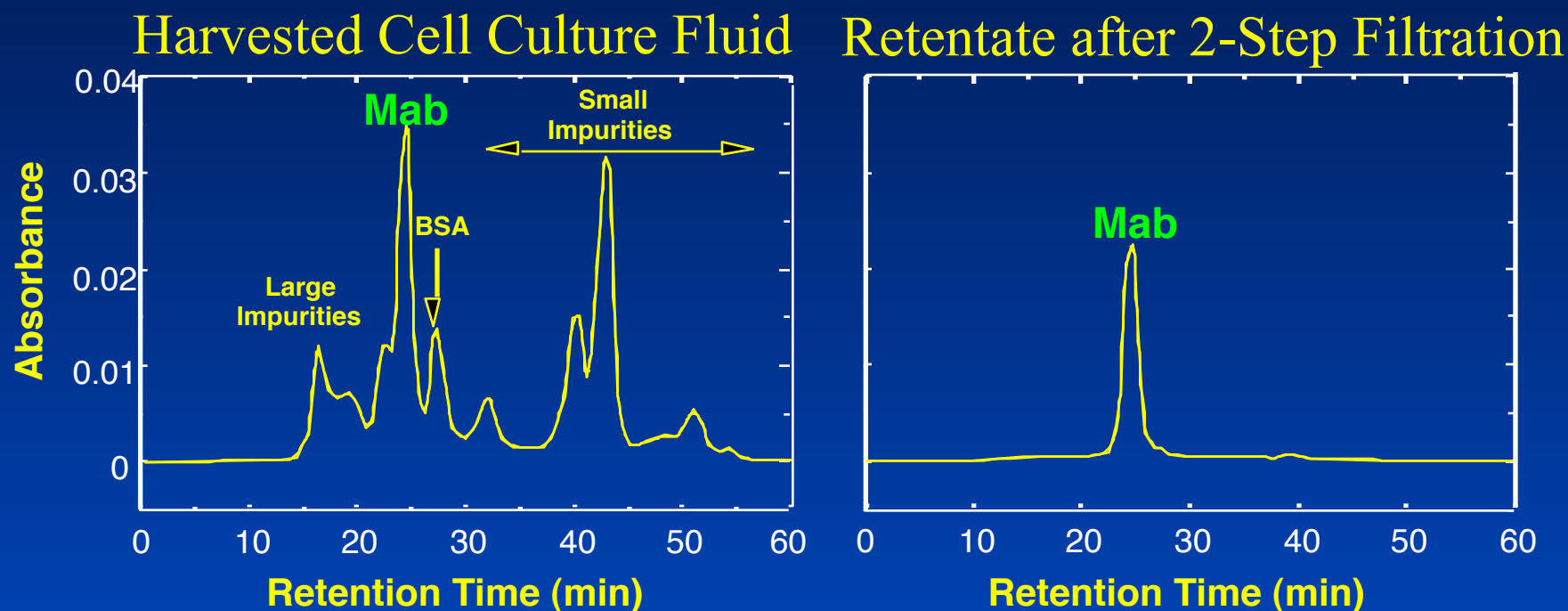
**Final filtrate**



Protein	MW (kD)	pI
$\beta$ -lactoglobulin	18	5.2
$\alpha$ -lactalbumin	14	4.6

*Cheang and Zydney, J Membrane Sci, 231, 159 (2004)*

# Monoclonal Antibody Purification from Harvested Cell Culture Fluid



- Purification with two membrane separations:
  - Step 1: pH 7, 150 mM phosphate (Mab in permeate)
  - Step 2: pH 4, 10 mM acetate (Mab in retentate)

# Membrane Transport

---

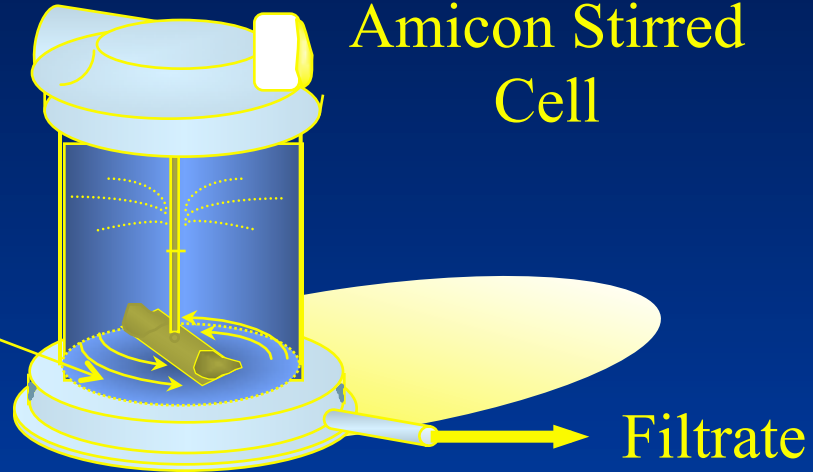
- Use of membranes for protein purification has generated renewed interest in understanding protein transport through semipermeable membranes
  - Diffusion / convection in highly constricted pores, including effects of pore geometry
  - Effects of electrostatic interactions (solution pH, ionic strength, membrane charge)


# Stirred Cell Apparatus

Air Pressure

Amicon Stirred Cell

Ultrafiltration Membrane



 The image cannot be displayed. Your computer may not have enough memory to open the image, or the image may have been corrupted. Restart your computer, and then open the file again. If the red x still appears, you may have to delete the image and then insert it again.

**Filtrate Flux:**

$$J_v = \frac{Q}{A}$$

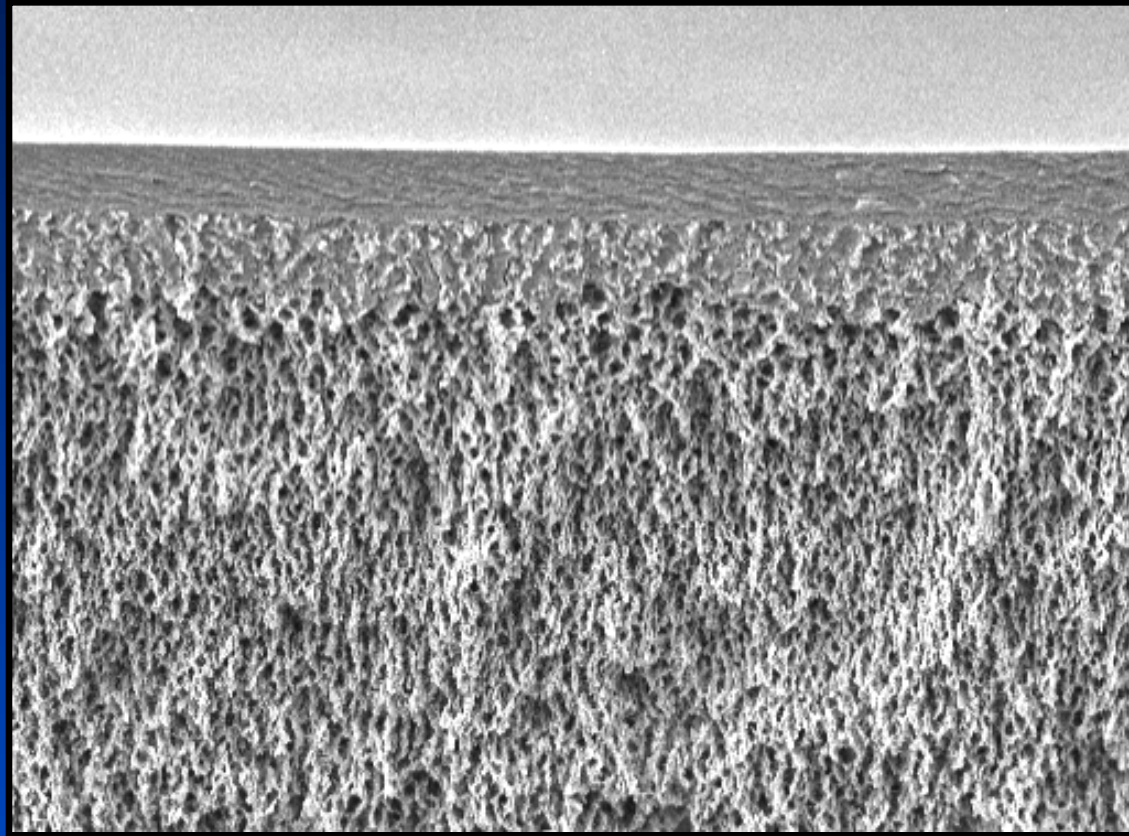
**Observed Sieving Coefficient:**

$$S_o = \frac{C_{filtrate}}{C_{bulk}}$$

PENNSSTATE



# Ultracel Membrane

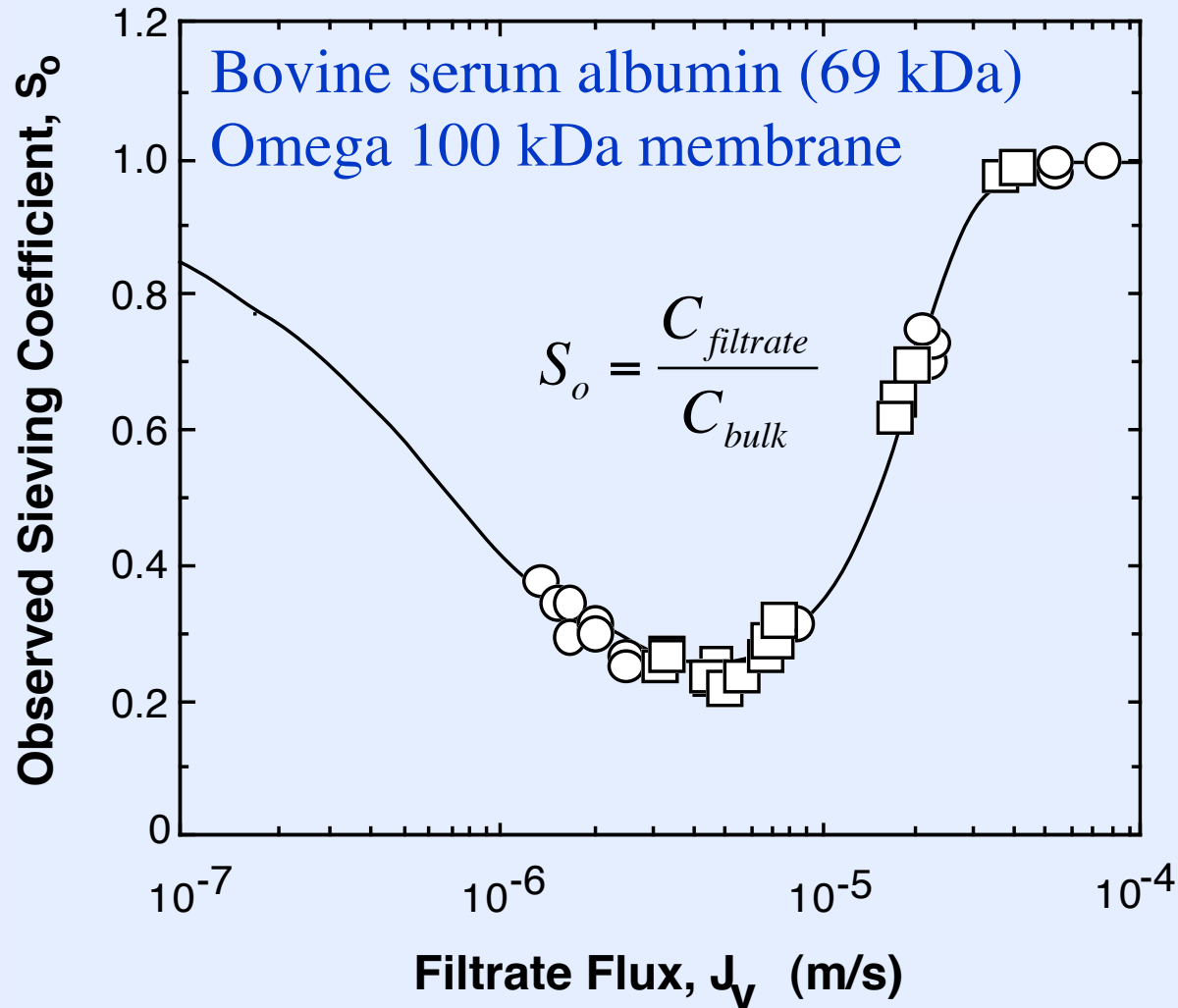


Skin

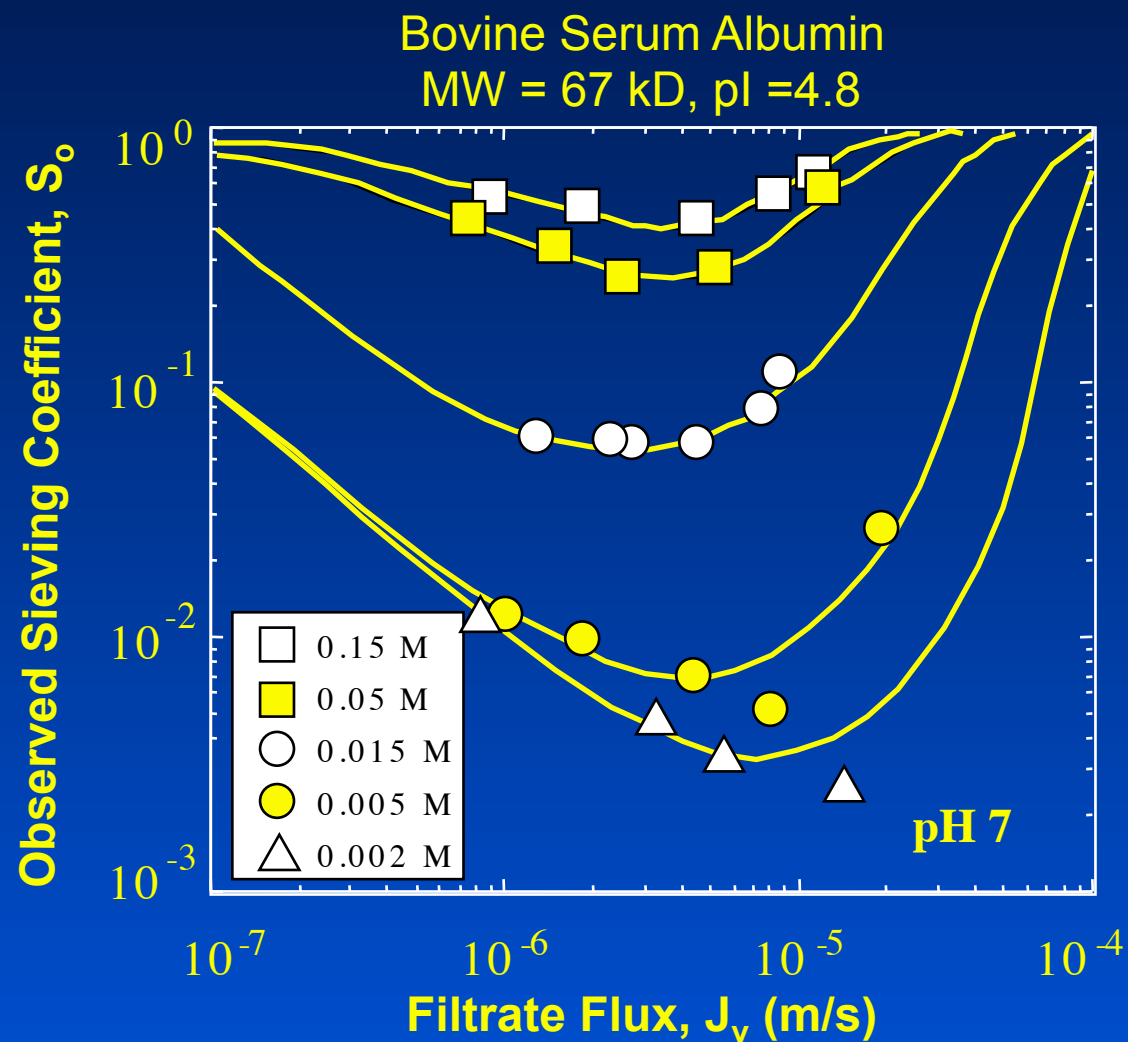
Support  
structure

- Composite regenerated cellulose membrane
- SEM cross-section provided by Millipore

# Sieving Coefficient vs Flux

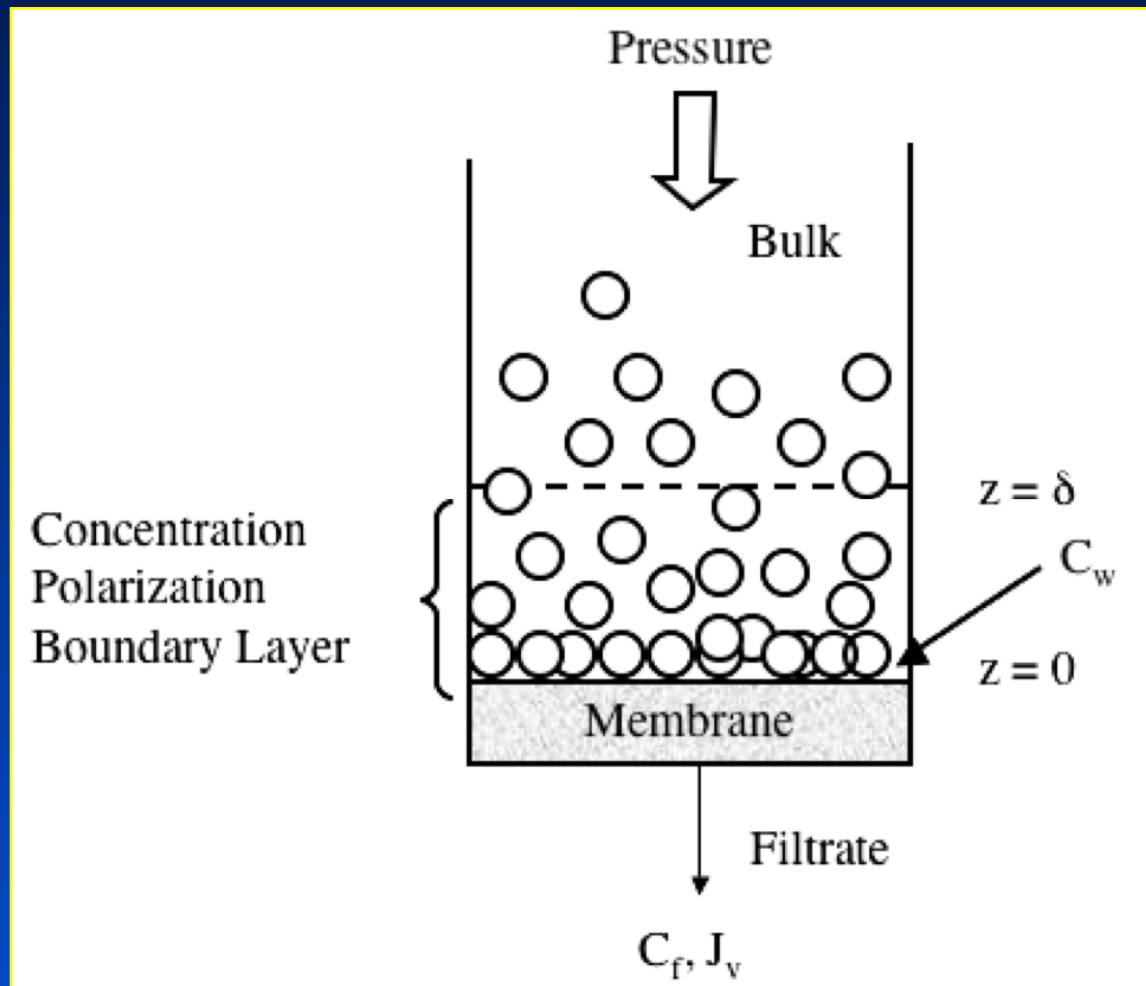


# Effect of Ionic Strength

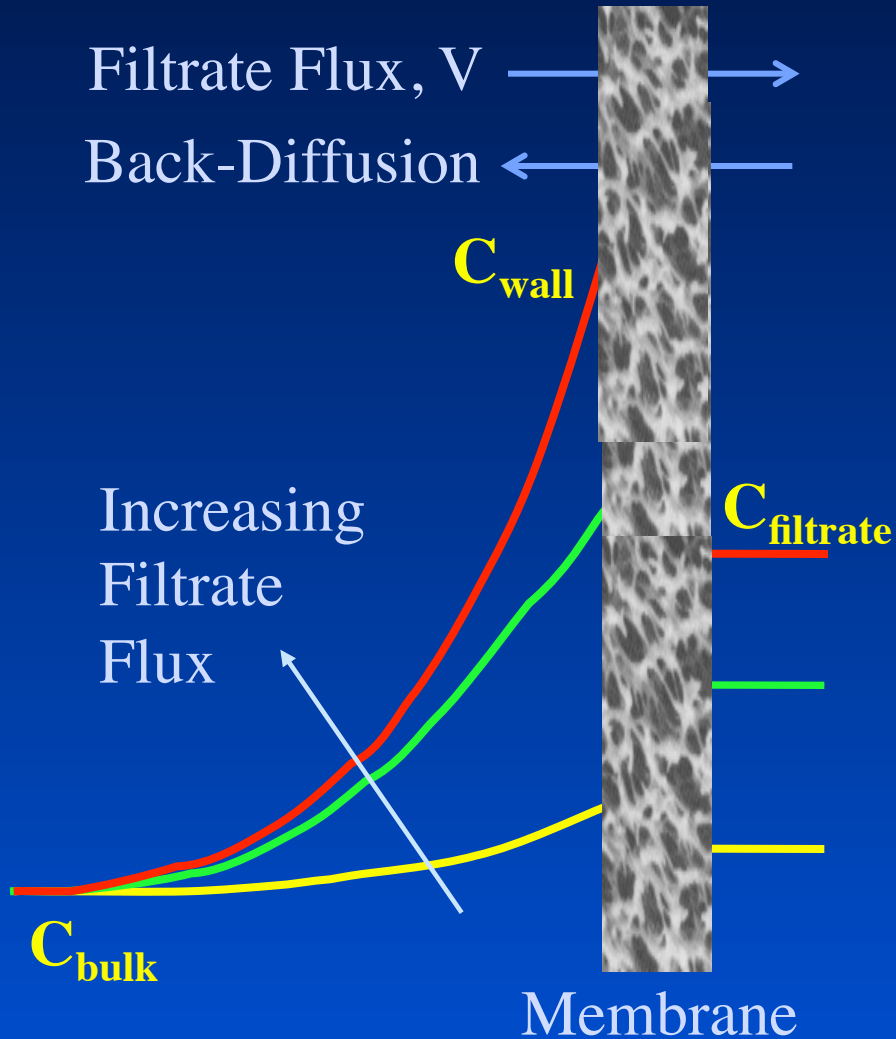




# Concentration Polarization



# Concentration Polarization

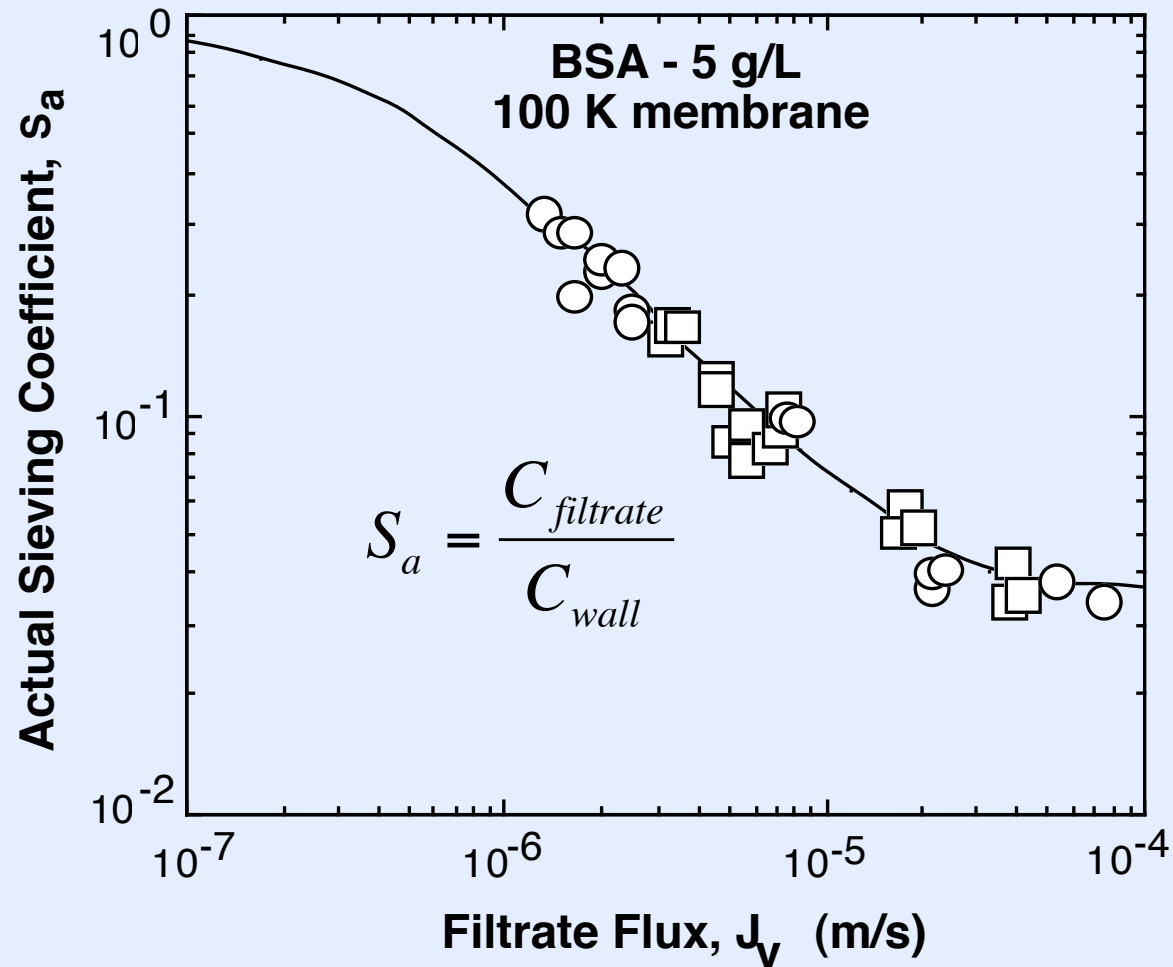


Accumulation of retained protein at upstream surface of membrane

- Extent of polarization determined by balance between convection towards membrane and diffusion back into bulk solution

$$VC - D_{\infty} \frac{\partial C}{\partial z} = VC_{filtrate}$$

# Actual Sieving Coefficient



# Membrane Transport

**Solute Flux:**

$$N_s = K_c V C_{pore} - K_d D_\infty \frac{\partial C_{pore}}{\partial z}$$

$K_c$  = hindrance factor for convection

$K_d$  = hindrance factor for diffusion

**Partition Coefficient:**

$$\phi = \frac{C_{pore, z=0}}{C_{wall}} = \frac{C_{pore, z=\delta_m}}{C_{filtrate}}$$

*Assumes equilibrium at pore entrance ( $z = 0$ )  
and pore exit ( $z = \delta_m$ )*

# Actual Sieving Coefficient

$$S_a = \frac{C_{filtrate}}{C_{wall}} = \frac{S_\infty \exp(Pe_m)}{S_\infty + \exp(Pe_m) - 1}$$

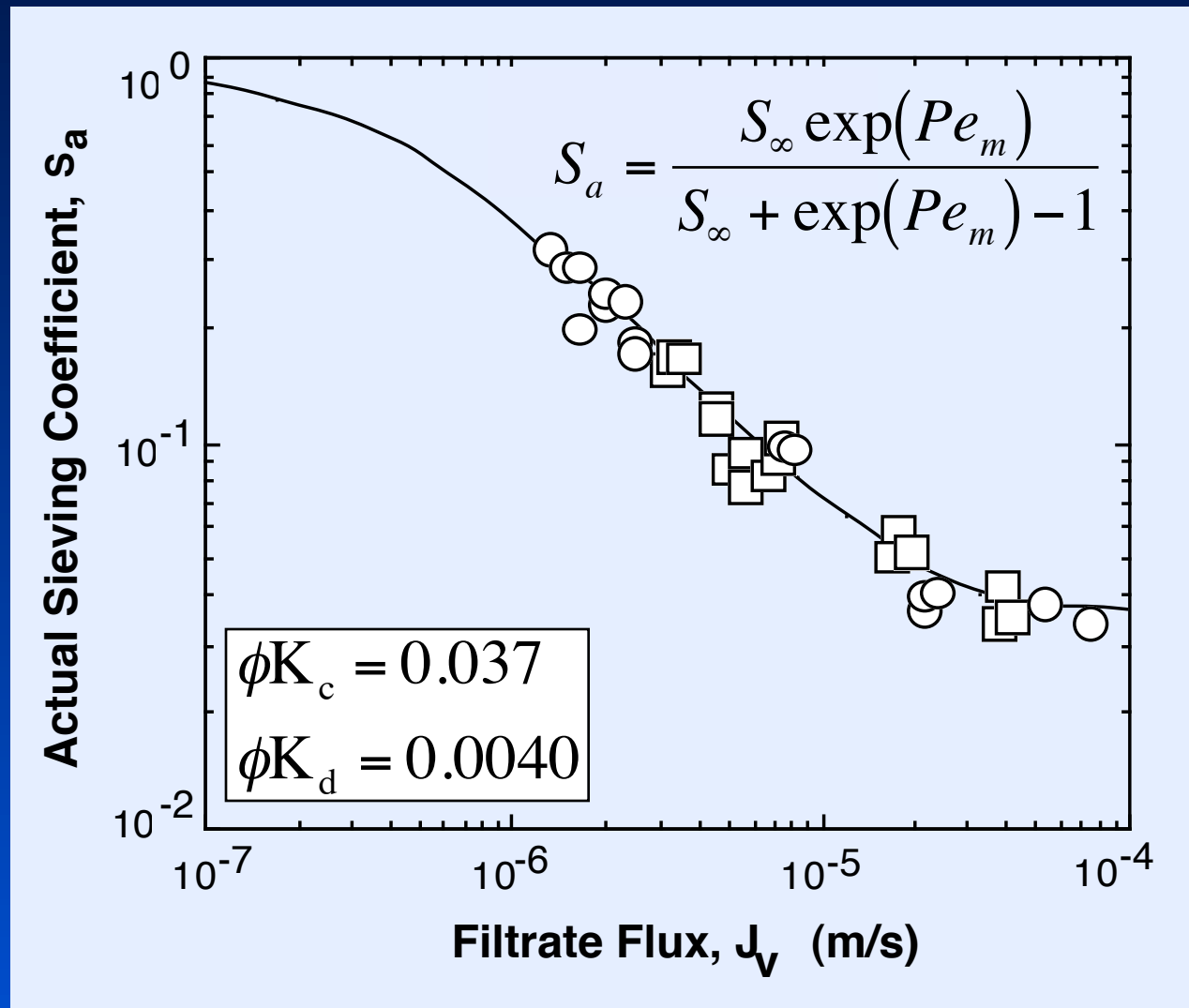
**Asymptotic Sieving Coefficient:**

$$S_\infty = \phi K_c$$

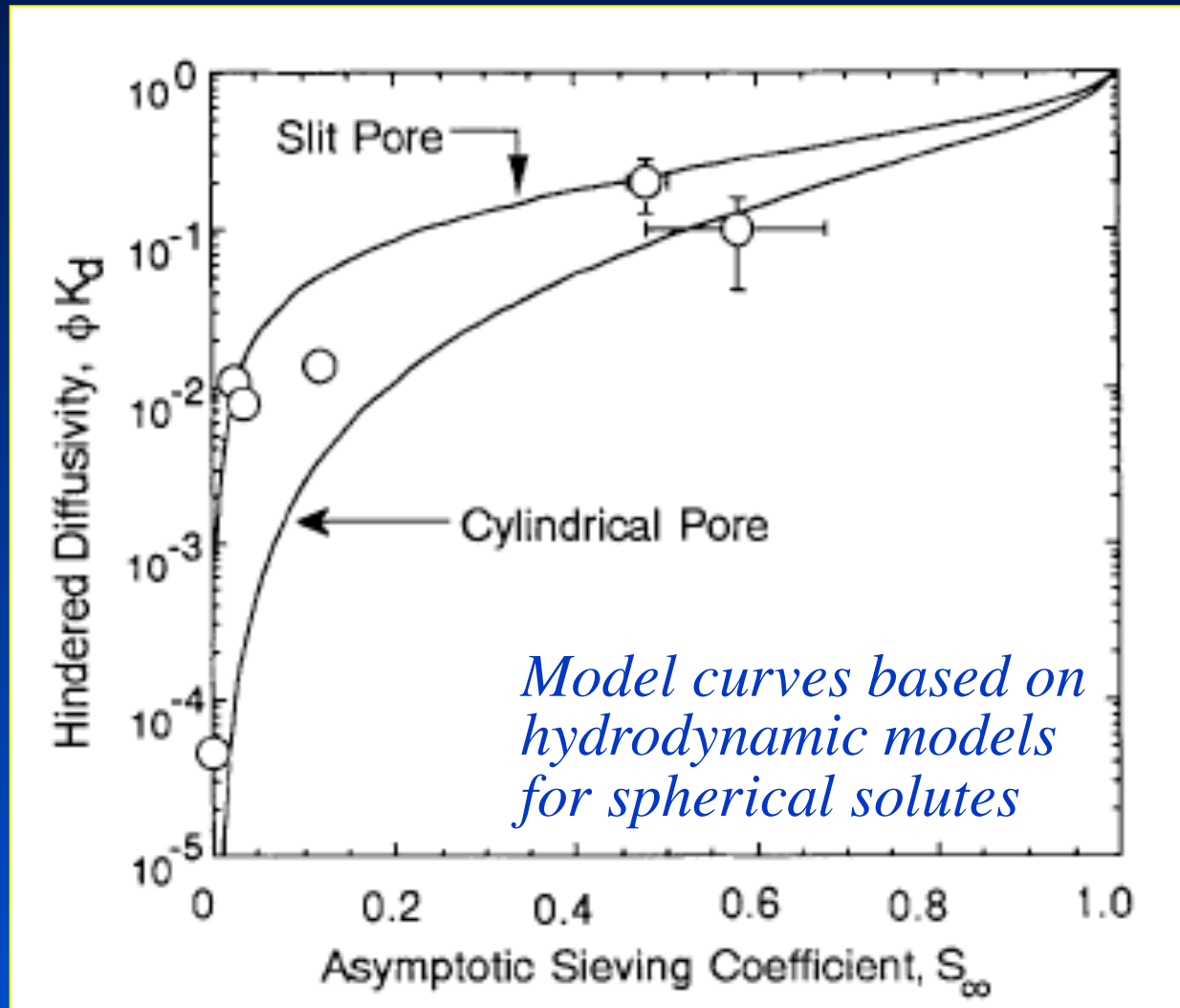
**Membrane Peclet Number:**

$$Pe_m = \frac{K_c}{K_d} \left( \frac{V \delta_m}{D_\infty} \right)$$

# Actual Sieving Coefficient



# Hindrance Coefficients



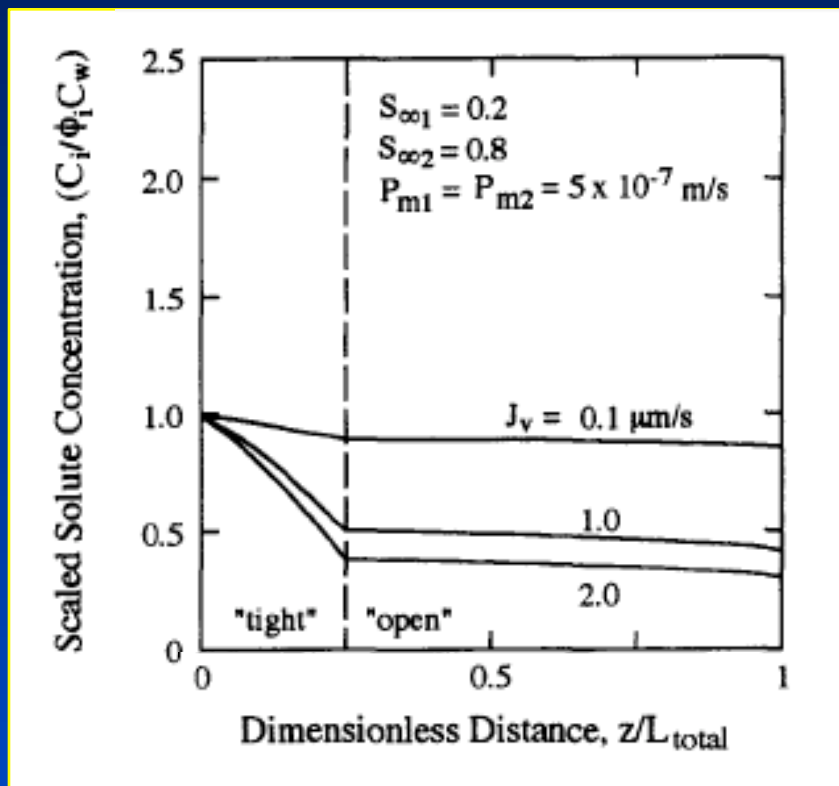
# Multi-layer Membranes

---

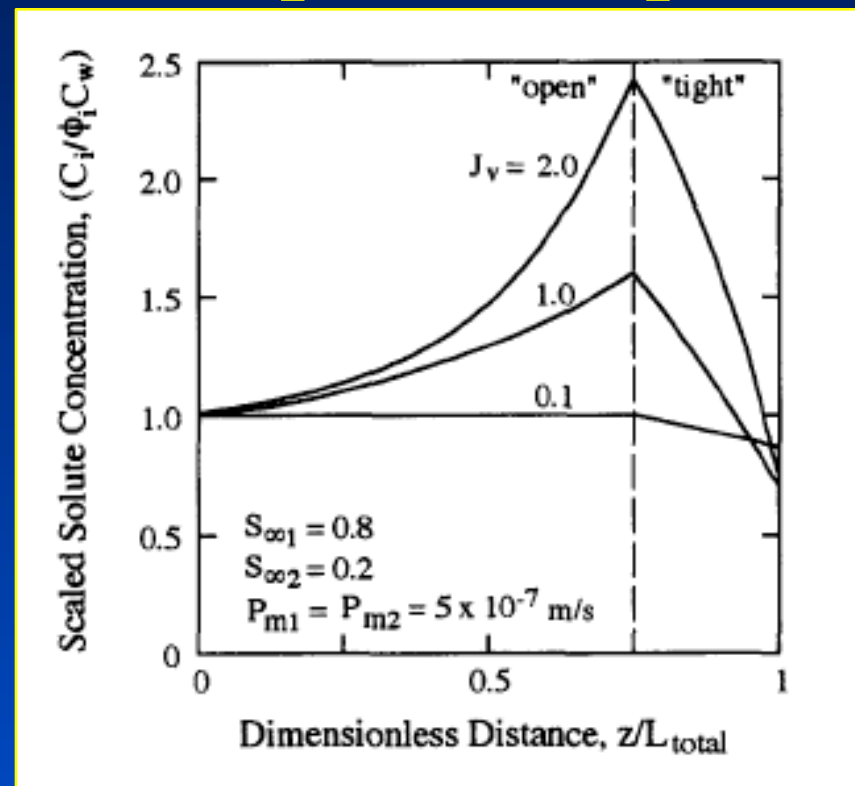
- Effects of diffusion / convection are significantly more complicated in multilayer and asymmetric membranes
  - Internal concentration polarization develops when flow is through the more open (larger pore size) region first
  - Net result is a directional dependence to solute transport / sieving coefficient

# Directional Dependent Transport

## Tight side up

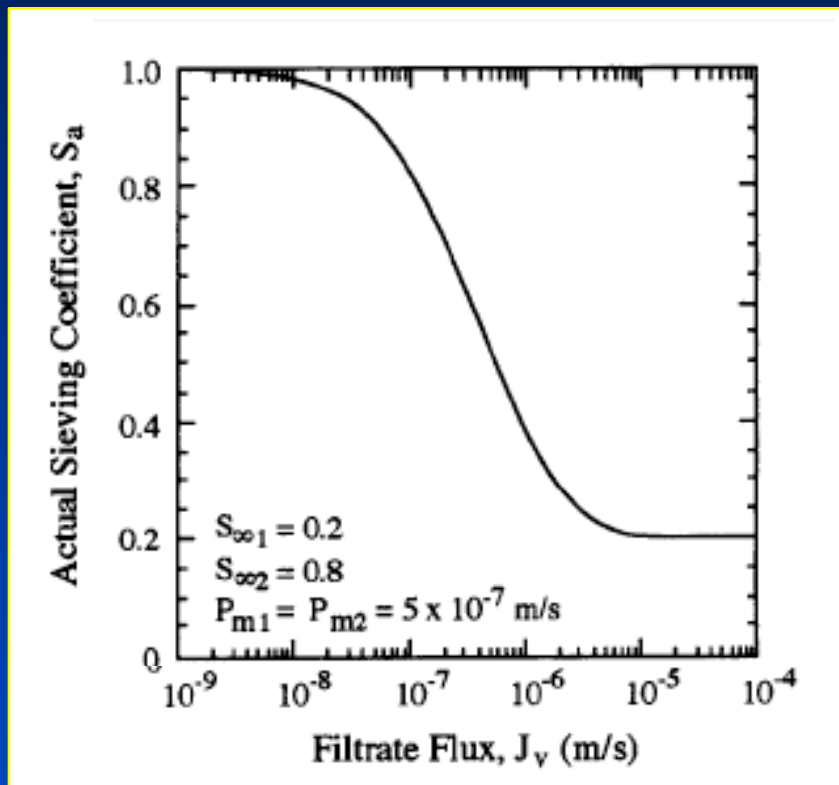


## Open side up

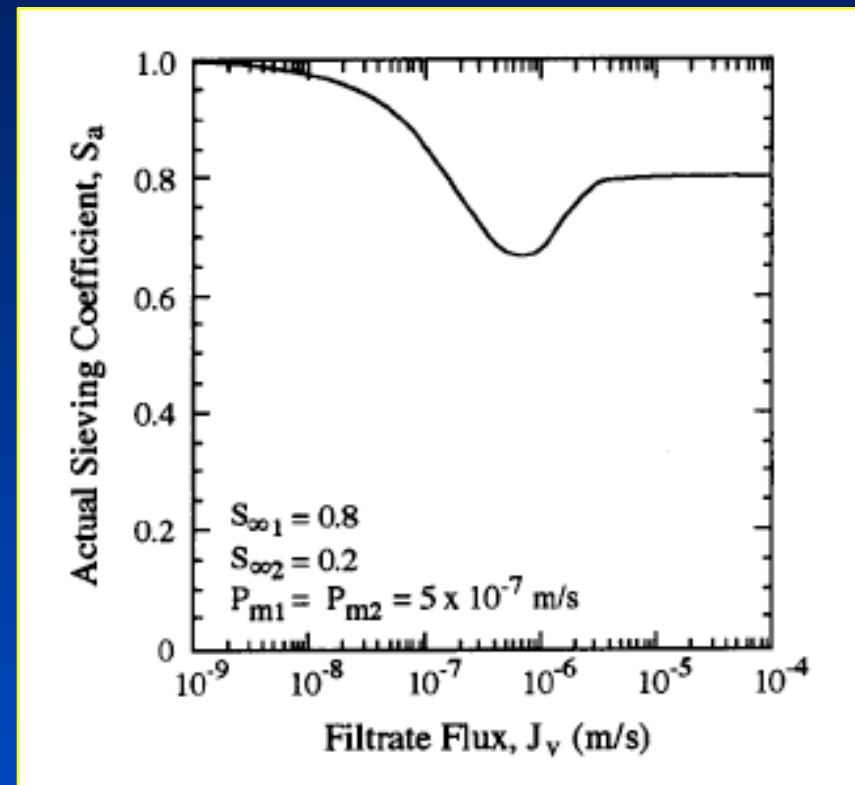


# Actual Sieving Coefficient: Two-Layer Membrane

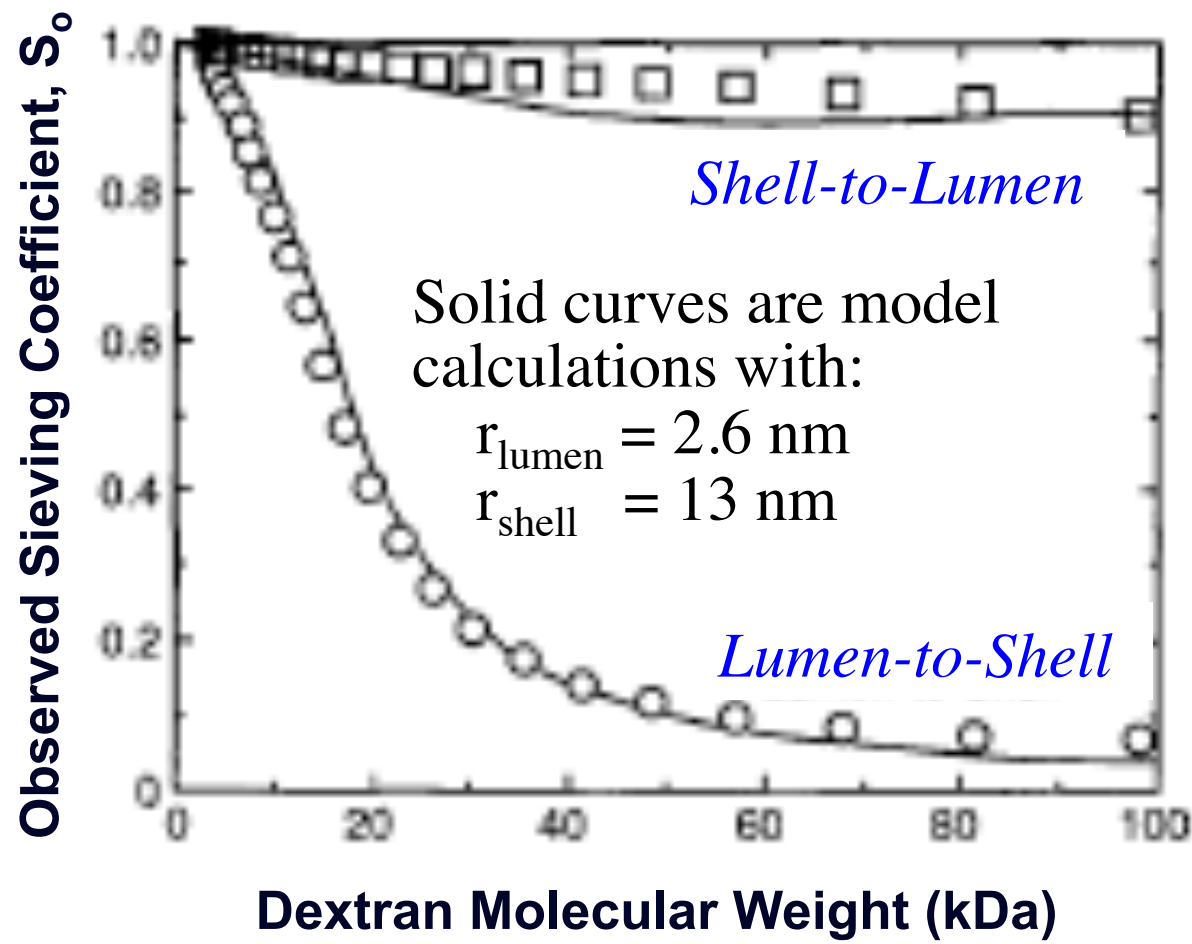
Tight side up



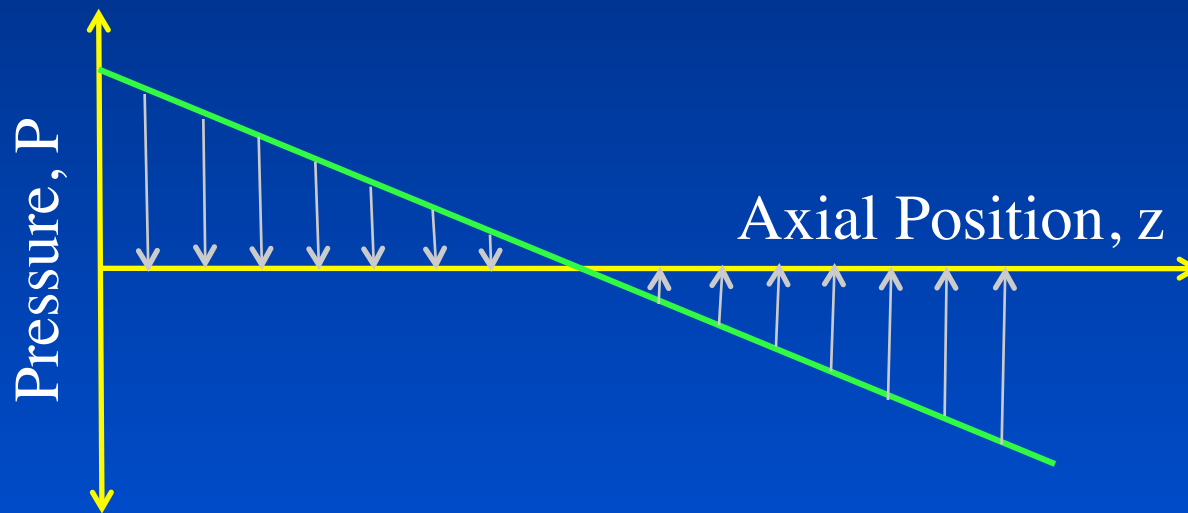
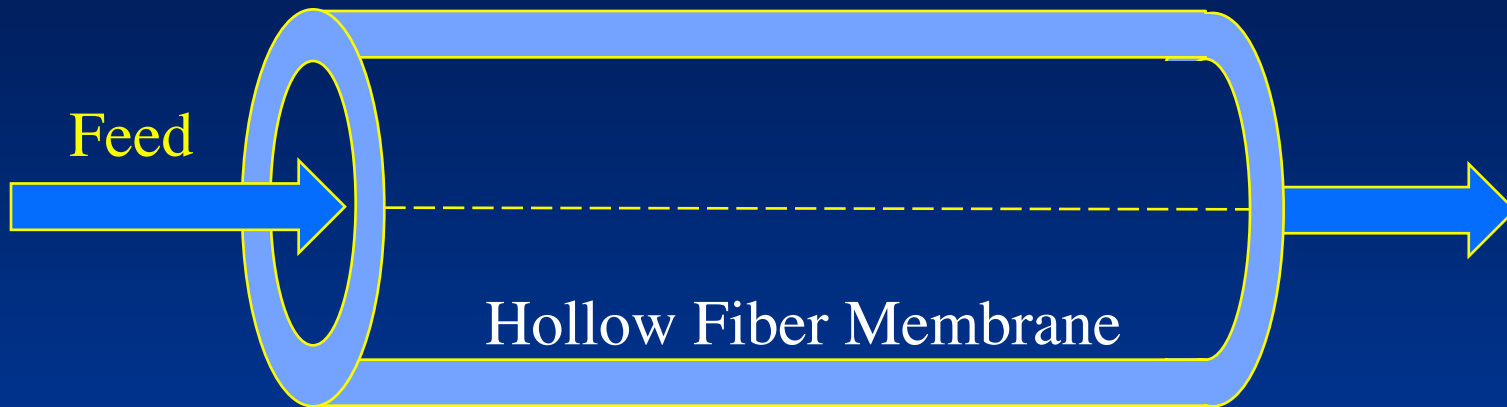
Open side up



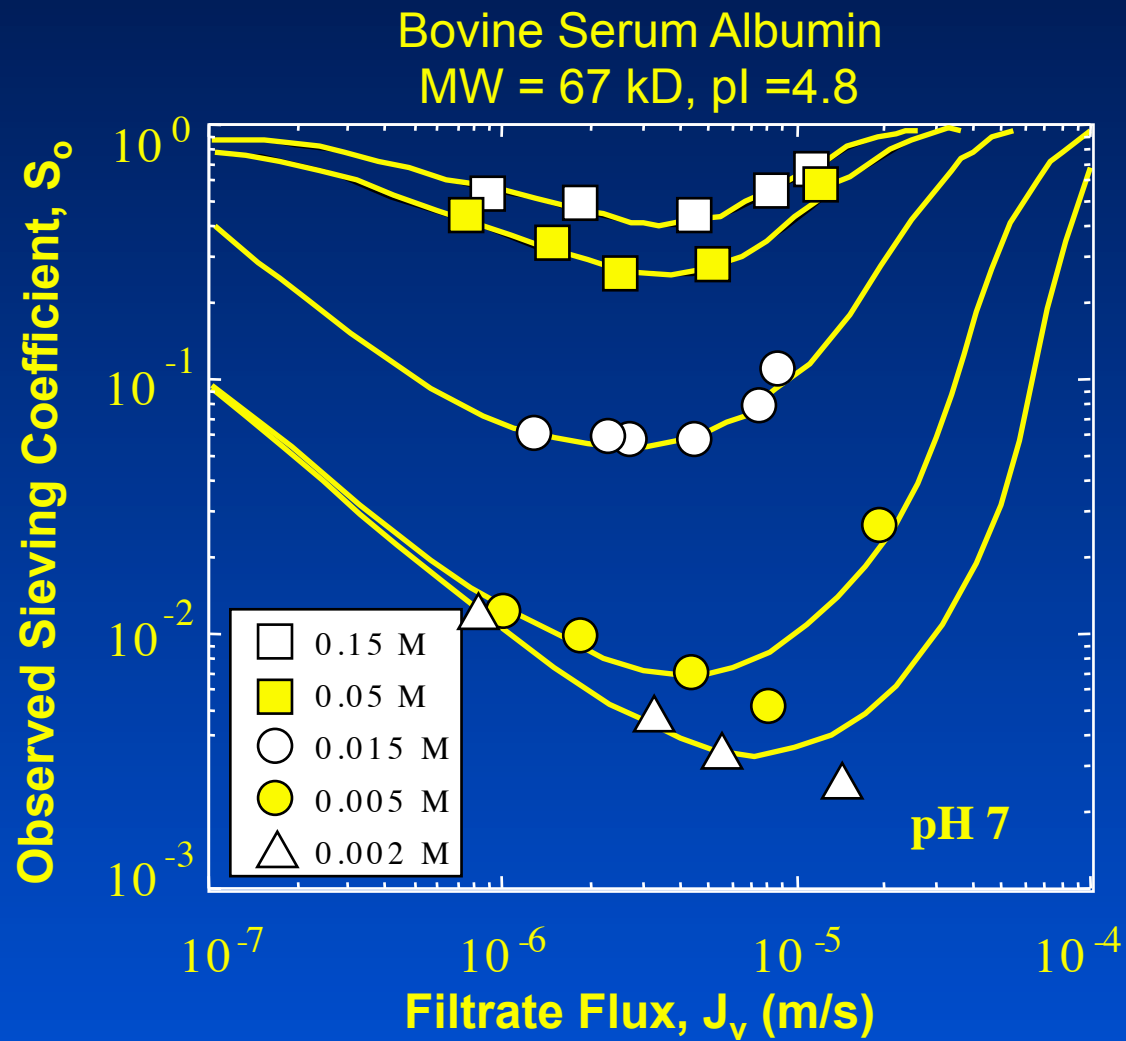
# Dextran Sieving – Dual Skinned Hollow Fiber Membrane



# Starling Flow - Backfiltration

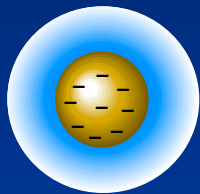


# Electrostatic Interactions



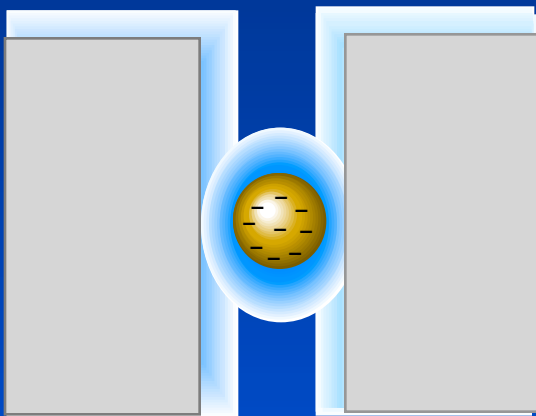
# Electrostatic Interactions

$$\phi = \frac{C_{\text{pore}}}{C_{\text{solution}}} = (1 - \lambda)^2 \exp\left(-\frac{E}{kT}\right)$$



↑  
steric  
interactions

↑  
electrostatic  
interactions



$$\lambda = \frac{r_{\text{solute}}}{r_{\text{pore}}} = \text{solute to pore size ratio}$$

$$\frac{E}{kT} = \text{dimensionless energy of interaction}$$

# Energy of Interaction

$$\frac{E}{kT} = A_1 \sigma_{protein}^2 + A_2 \sigma_{pore}^2 + A_3 \sigma_{protein} \sigma_{pore}$$

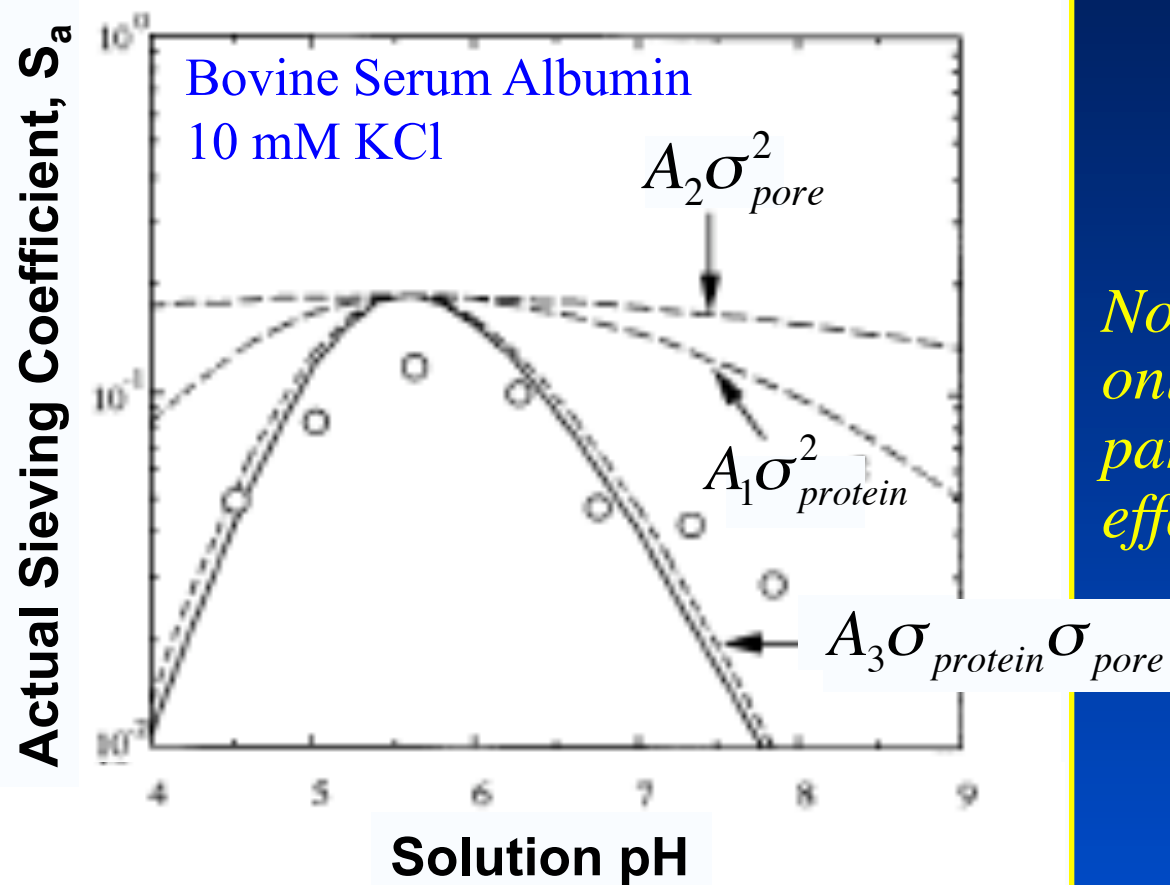
$\sigma_{protein}$  = surface charge density of protein

$\sigma_{pore}$  = surface charge density of pore wall

## Three terms associated with:

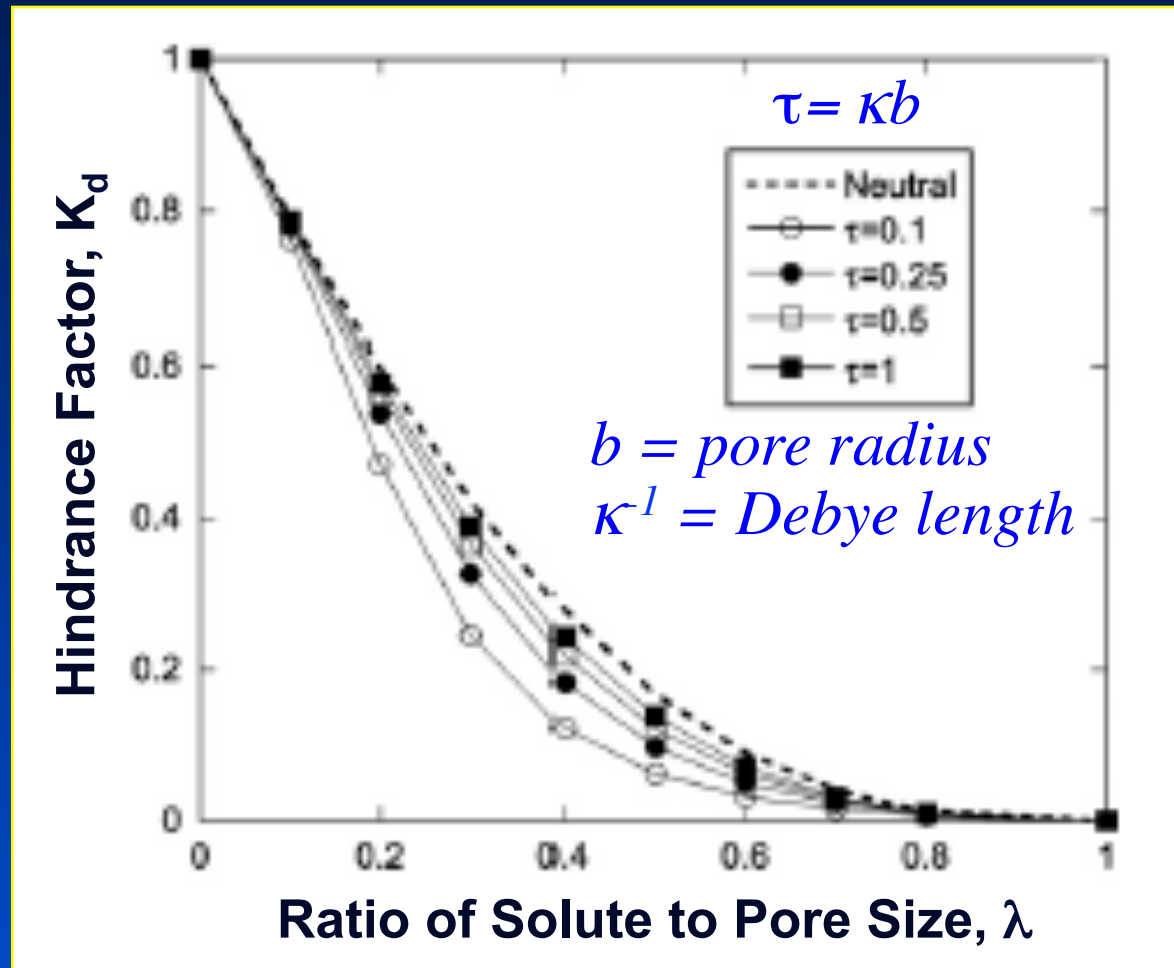
- (1) distortion of protein double layer
- (2) distortion of double layer in pore
- (3) direct charge-charge interactions

# Protein Sieving -- pH Effects



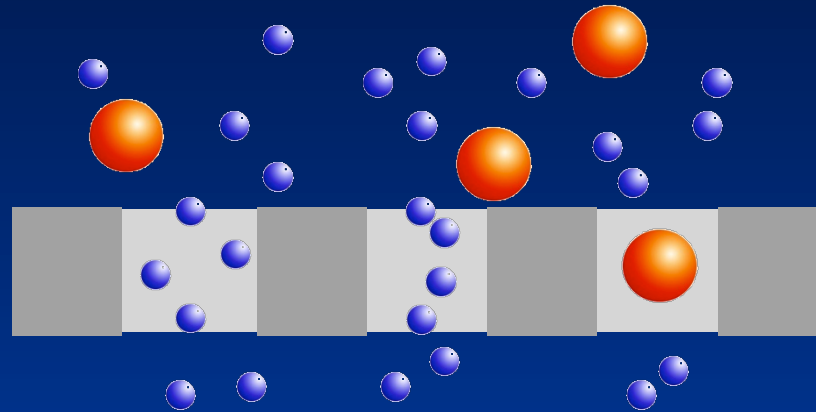
*Note: Model only includes partitioning effects*

# Hindrance Factor - Diffusion



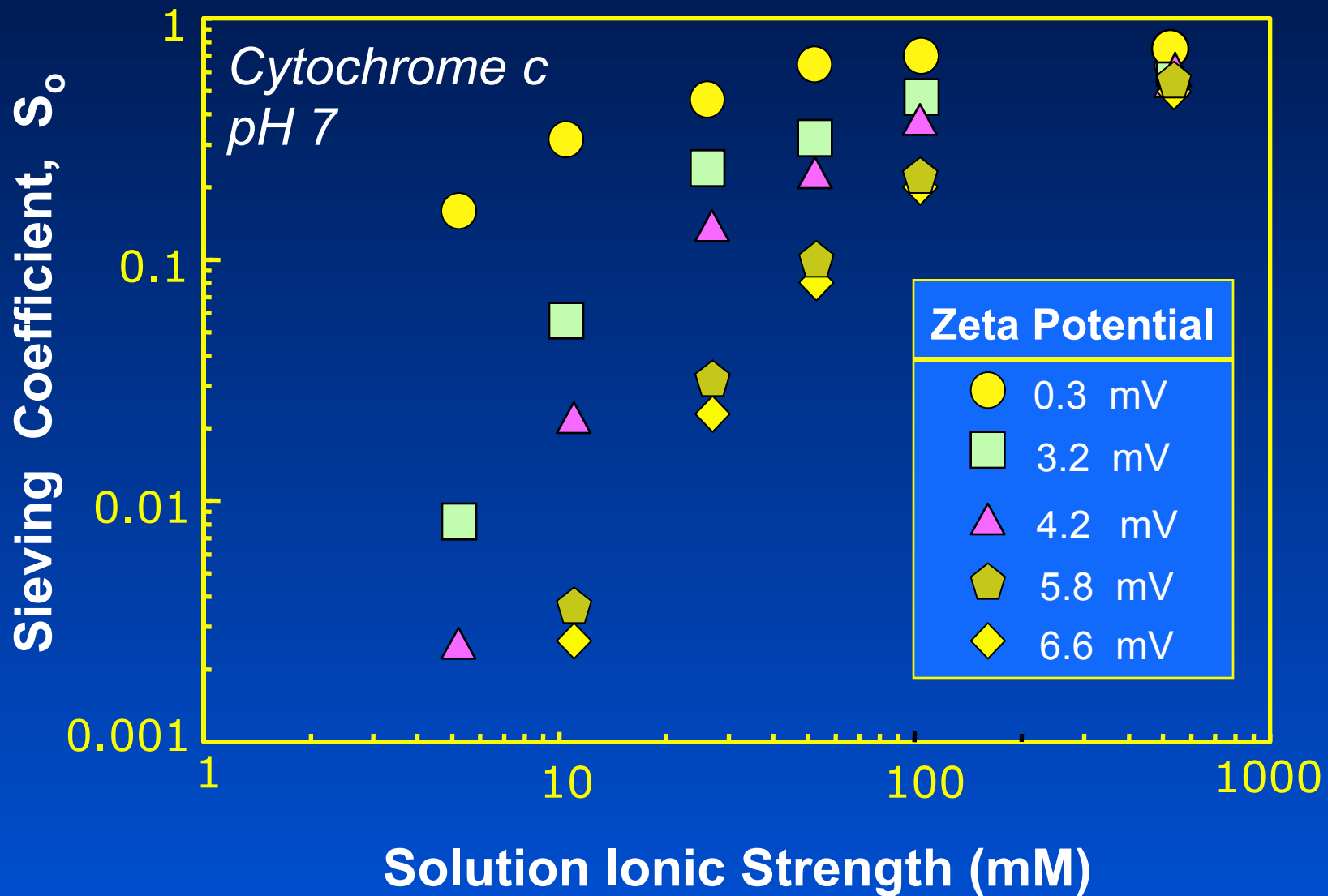
*from Dechadilok and Deen, J Membrane Sci, 336, 7 (2009)*

# Charged Membranes

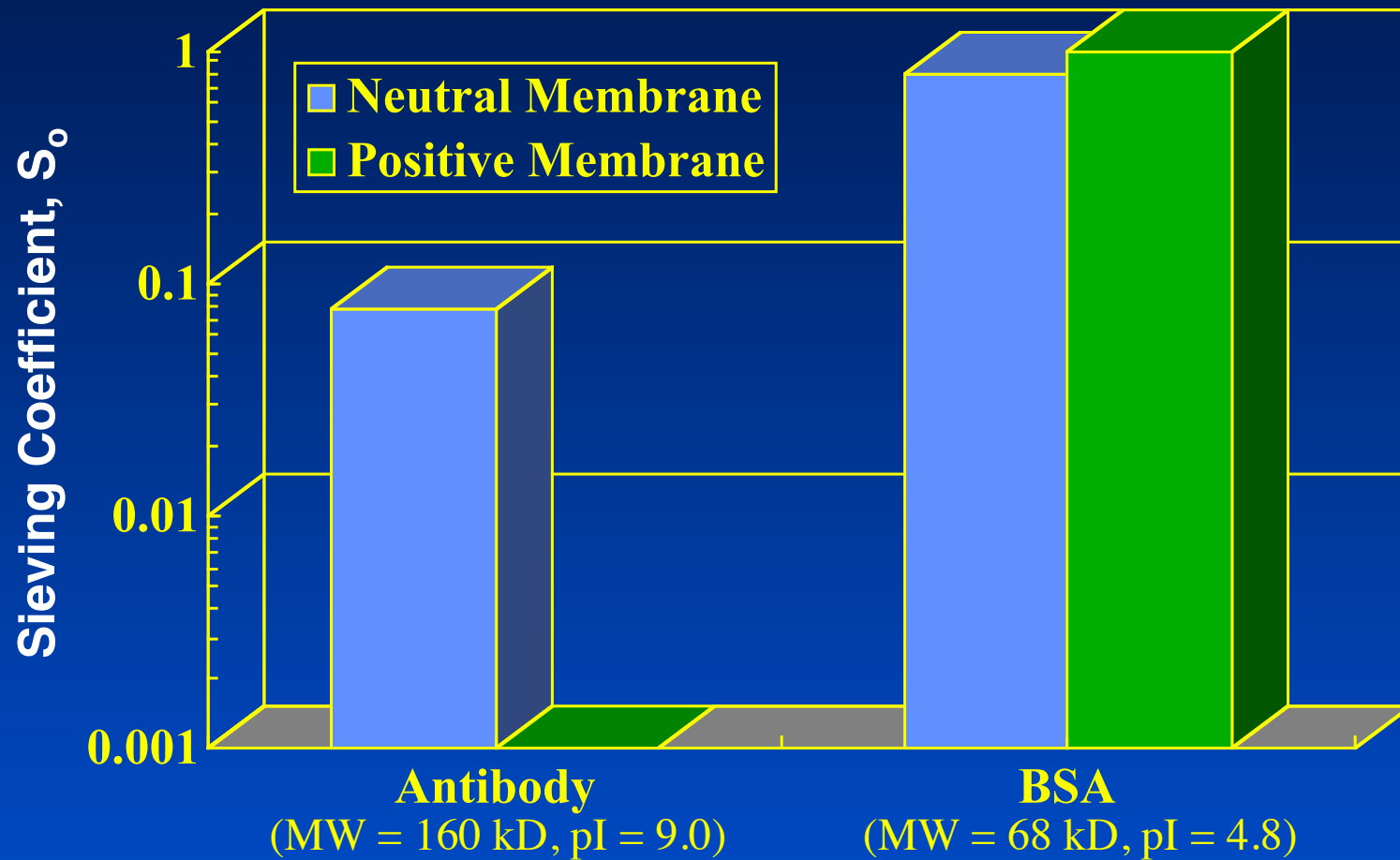


- Opportunity to improve performance of traditional ultrafiltration processes by increasing protein retention
- Opportunities for highly-selective protein separations

# Membrane Charge Effects



# Membrane Charge Effects



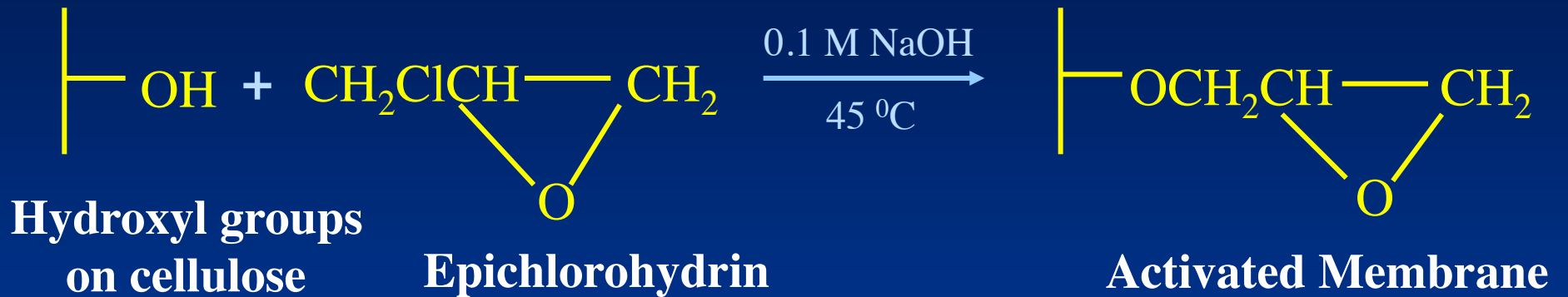
*pH 5.0, 10 mM acetate buffer*

# Charged UF Membranes

---

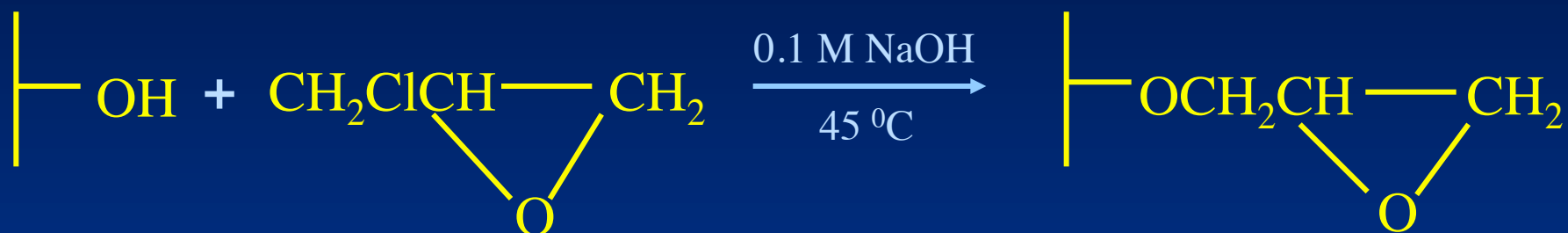
- **Number of Charge Groups**
  - Surface density of ligands
  - Ligands with multiple charge groups
- **Location of Charge Groups**
  - Effect of spacer arm length / branching
- **Nature of Charge Groups**
  - Weak versus strong acid / base
  - Detailed ligand and linkage chemistry

# Epichlorohydrin Activation



*Degree of modification controlled by reaction time*

# Diamine Addition



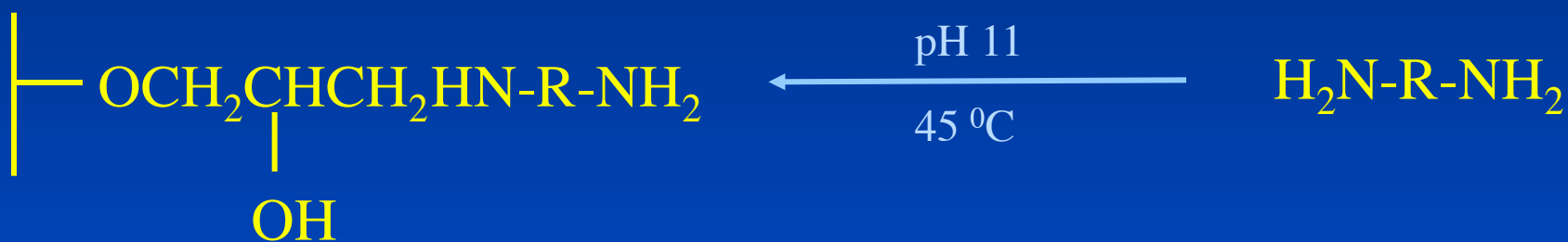
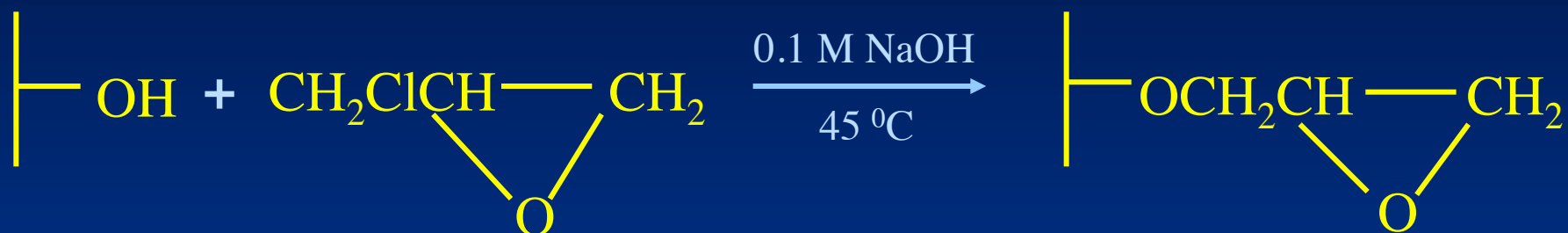
+



Diamine

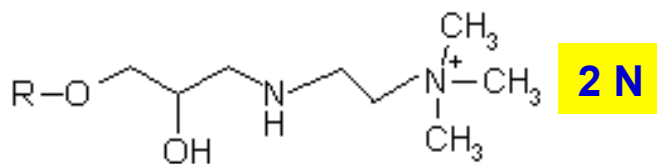
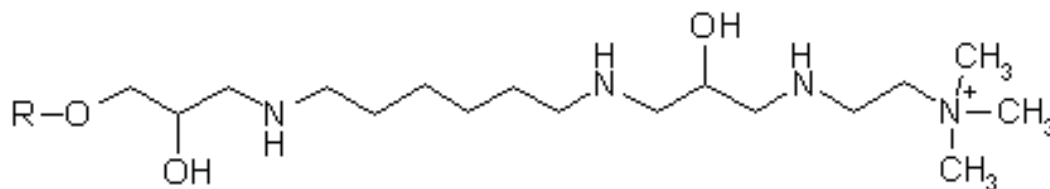
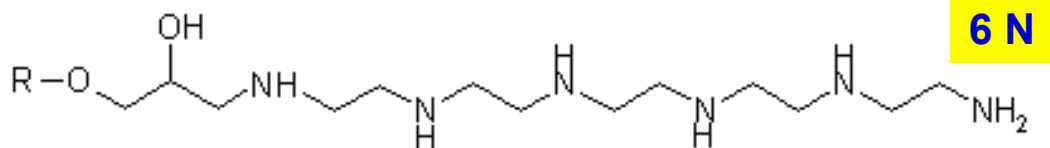
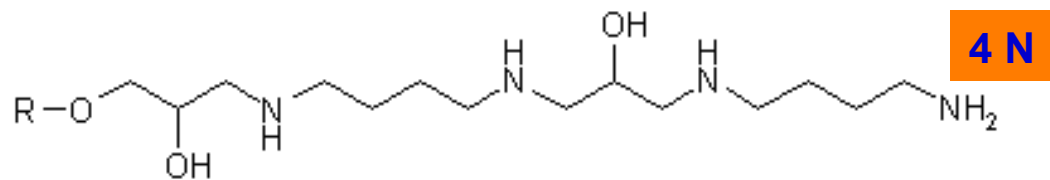
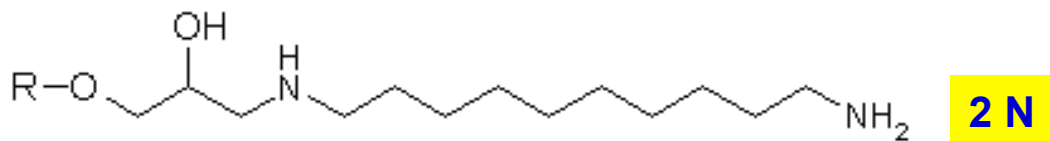
*Multiple chemistries  
and ligand lengths*

# Charge - Modified Membrane



Charge-Modified Membrane

# Ligand Chemistry



**(a) Diaminodecane**  
(1.4 nm), 13 C

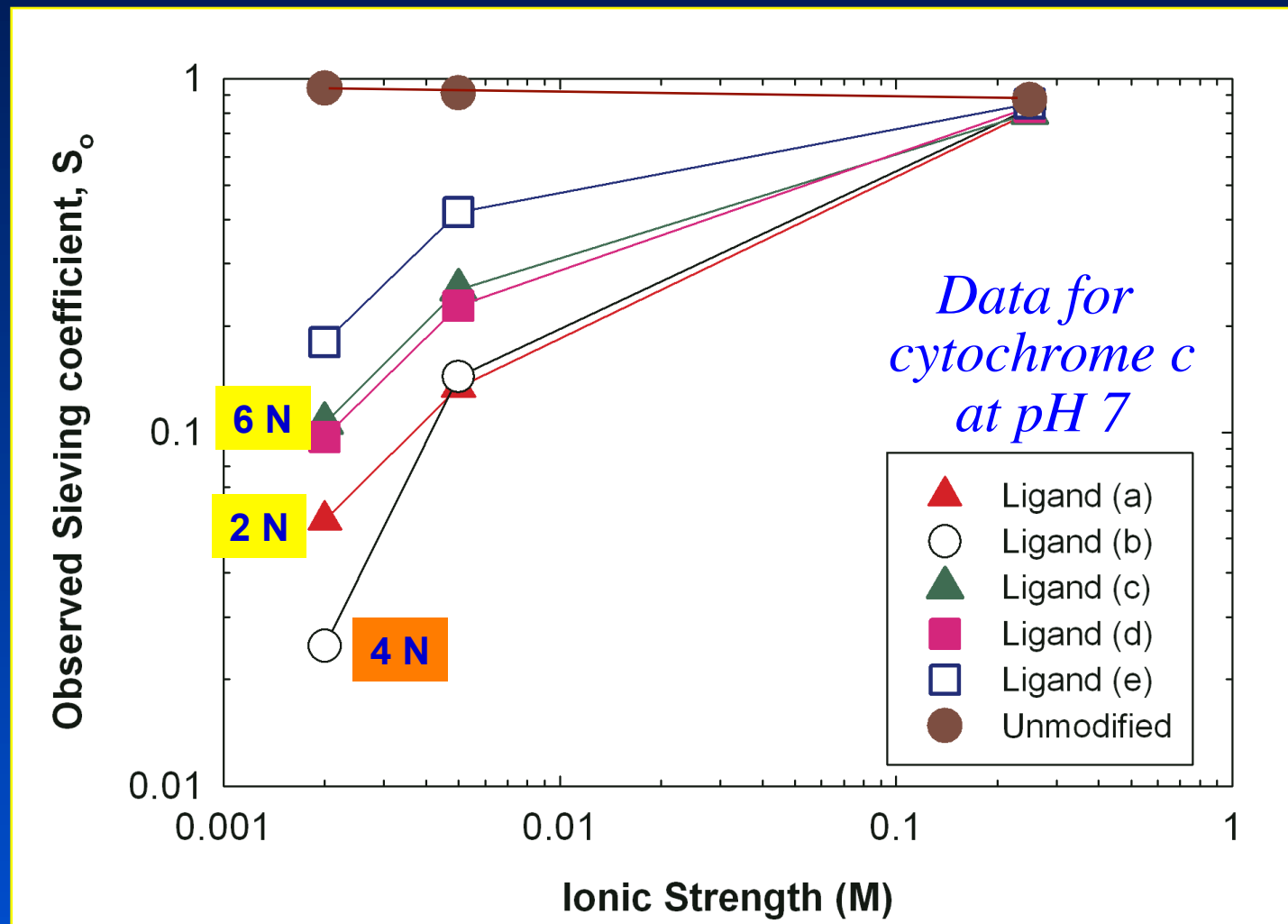
**(b) Diaminobutane**  
(1.8 nm), 14 C  
*Sequential reaction*

**(c) Pentaethylenhexamine**  
(1.8 nm), 13 C

**(d) Quaternary amine**  
(1.7 nm), 14 C  
*Sequential reaction*

**(e) Short quaternary amine**  
(0.4 nm), 5 C

# Effects of Ligand Chemistry



# Separation of Protein Variants

---

- Protein variants differ at only a single amino acid residue (e.g., deamidation, oxidation of methionine, carbamylation, etc)
- Resulting variants can have different activity and immunogenicity --> very challenging separation
- **Example:** myoglobin variants produced by chemical modification of a single lysine (conversion of amine to carboxylic acid)

# Myoglobin Sequence

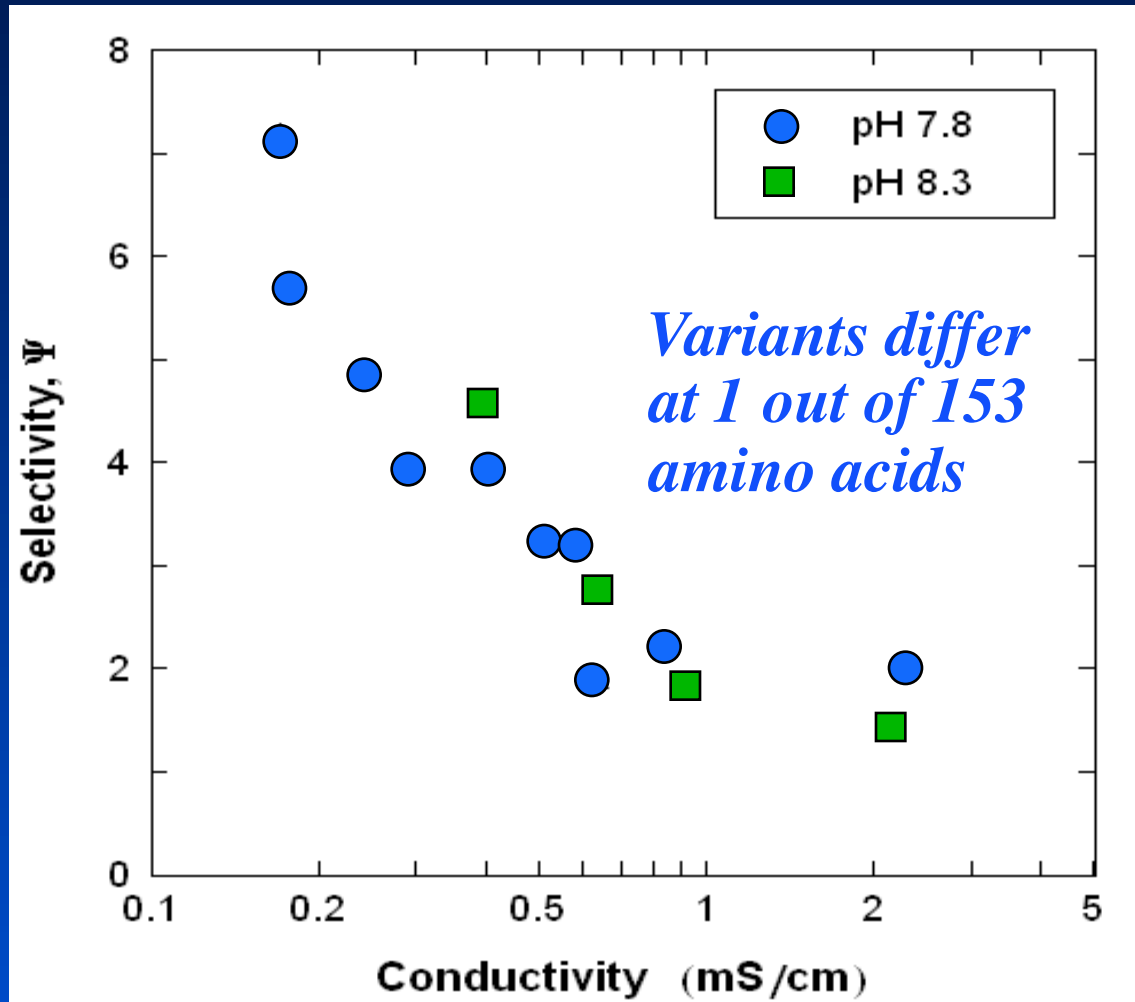
---

GLSDGEWQQV  
IAGHGQEVLI  
EKFDKFKHLK  
LKKHGTVVLT  
HHEAELKPLA  
IKYLEFISDA  
GDFGADAQGA  
DIAAKYKELG

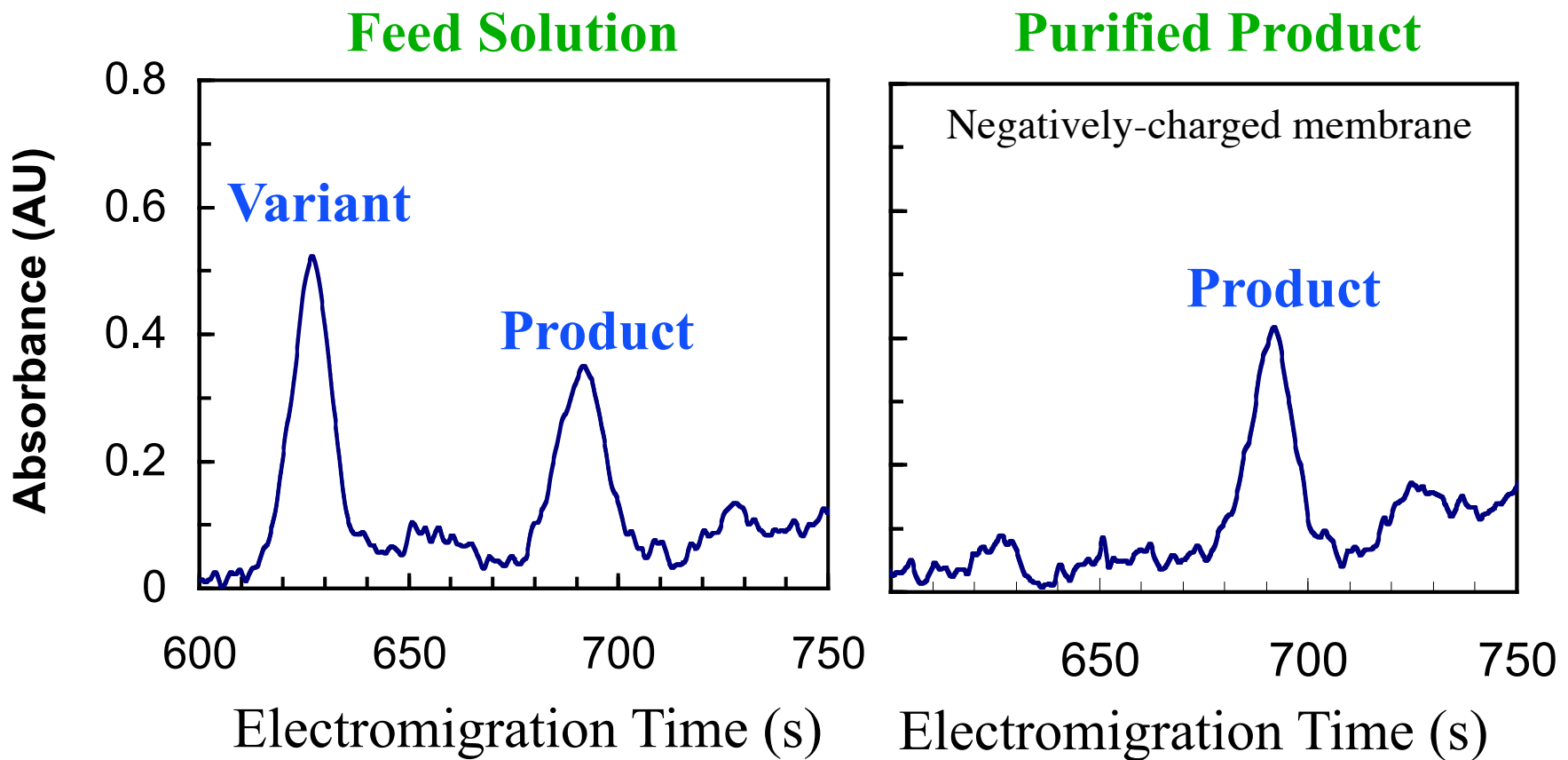
LNVWGKVEAD  
RLFTGHPETL  
TEAEMKASED  
ALGGILK(K)KG  
QSHATKHKIP  
IIHVLHSKHP  
MTKALELFRN  
FQG

*Chemical modification of a single lysine amino acid  
out of 153 residues*

# Selectivity for Myoglobin Variants



# Separation of Myoglobin Variants



# Summary

---

- **Diffusive transport can significantly alter protein transmission during ultrafiltration**
  - Bulk mass transport (concentration polarization)
  - Enhanced transmission at low filtrate flux
  - Directional dependence for multilayer membranes
- **Electrostatic interactions provide unique opportunities for enhanced performance**
  - Repulsive interactions cause strong rejection
  - Role of ligand structure still being explored

# Acknowledgements

---

## Penn State

- Amit Mehta (Genentech)
- Russell Boyd (Merck)
- Doug Burns (Talecris)
- Mareia Ebersold
- Mahsa Rohani

## Genentech

- Robert van Reis

## Millipore

## Baxter Healthcare

## Financial Support

- Millipore - *Ultracel Membranes*
- Walter L. Robb Family Chair