Universität Leipzig, Fakultät für Physik und Geowissenschaften

## Exercises for Experimental Physics 1 – IPSP Prof. Dr. J. Käs, Dr. M. Zink Exercise Sheet 10 (WS 2011/12)

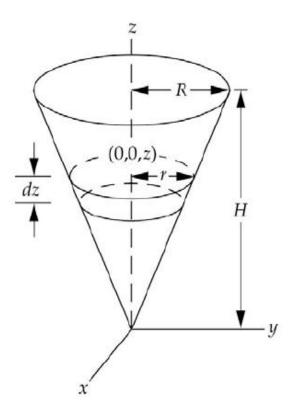
Date of Issue:Dec.  $9^{th}$  2011Date of Submission:Dec.  $16^{th}$  2011

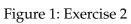
**Submission Place:** Marked mailbox next to room 302 (Linnestr. 5) **Submission Time:** 11:00 a.m. at the submission day noted above

Please note: Write your name and matriculation number on EACH sheet of paper. Only submit the calculations and results for exercise 1-3, exercise 4 will be discussed during the instruction classes.

## **Exercises:**

- 1. Two point masses  $m_1$  and  $m_2$  are separated by a massless rod of length *L*. (a) Write an expression for the moment of inertia *I* about an axis perpendicular to the rod and passing through it a distance *x* from mass  $m_1$ . (b) Calculate dI/dx and show that *I* is at a minimum when the axis passes through the center of mass of the system. (6 Points)
- 2. Use integration to determine the moment of inertia about its axis of a uniform right circular cone of height *H*, base radius *R*, and mass *M*. Use Figure 1. (7 Points)
- 3. A uniform horizontal disk of mass *M* and radius *R* is spinning about the vertical axis through its center with an angular speed  $\omega$ . When the spinning disk is dropped onto a horizontal tabletop, kinetic-frictional forces on the disk oppose its spinning motion. Let  $\mu_k$  be the coefficient of kinetic friction between the disk and the tabletop. (a) Find the torque  $d\tau$  exerted by the force of friction on a circular element of radius *r* and width *dr*. (b) Find the total torque exerted by friction on the disk. (c) Find the time required for the disk to stop rotating. (7 Points)
- 4. As the chief design engineer for a major toy company, you are in charge of designing a "loop-the-loop" toy for youngsters. The idea, as shown in Figure 2, is that a ball of mass m and radius *r* will roll down an inclined track and around the loop without slipping. The ball starts from rest at a height *h* above the tabletop that supports the whole track. The loop radius is *R*. Determine the minimum height *h*, in terms of *R* and *r*, for which the ball will remain in contact with the track during the whole of its loop-the-loop journey. (Do not neglect the size of the ball's radius when doing this calculation.)





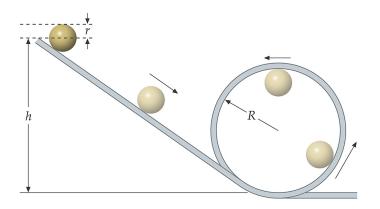


Figure 2: Exercise 4